

# Welcome!

This is the first in a series of teaching aids designed **by** teachers **for** teachers at level 5. The worksheets are designed to support the delivery of the National Curriculum in a variety of teaching and learning styles. They are not designed to take the pedagogy away from the teacher. The worksheets are centred around the shown level, but spiral from the level below to the level above. Consult the National Numeracy Strategy for definitive National Curriculum levels. They can be used by parents with the support of the on-line help facility at [www.10ticks.co.uk](http://www.10ticks.co.uk).

## Contents and Teacher Notes.

- Pages 3/4. **Grid Multiplication 1.**  
Pupils may be coming from Primary schools using this technique for multiplying numbers. It is particularly useful for long multiplication as it is clear where numbers belong. When pupils are particularly comfortable with this techniques, then they should be taught the more concise, traditional method. Less able pupils may never progress to traditional long multiplication.
- Pages 5/6. **Grid Multiplication 2.**  
Grid multiplication with missing numbers.
- Pages 7/8. **Long Multiplication.**  
A quick reminder of the usual level 4 multiplying before a traditional style level 5 exercise.
- Pages 9/10. **Long Division.**  
The first side is level 4 division as this is the one pupils normally forget, before a traditional style exercise on level 5 long division.
- Pages 11/12. **Long Multiplication and Division Problems.**  
Putting the skills pupils have learnt into context with worded questions.
- Pages 13/14. **Egyptian Multiplication/Russian Multiplication.**  
Ways other countries attempt long multiplication.
- Page 15. **Chinese Multiplication.**  
Another alternative way for long multiplication.
- Pages 16/17. **Spiralling Sums.**  
Long multiplications. Answers are written in words in a spiral grid. Shaded squares then read out mystery countries.
- Pages 18/19. **The Number 6/7 Multiple Maze.**  
Work out the sum, see if it is a multiple of the given number and try to find your way through the maze. The complexity of the two tasks combined gives it the level 5 rating !
- Pages 20/21. **The Number 8/9 Multiple Maze.**  
Work out the sum, see if it is a multiple of the given number and try to find your way through the maze. The complexity of the two tasks combined gives it the level 5 rating !
- Page 22. **Multiplication and Division Cross Numbers.**  
Three number "crosswords" using multiplication and division skills.
- Pages 23/24. **Prime Numbers 1.**  
A reminder about multiples and factors. Using factors as the definition of prime numbers. Introducing indices, leading to square and cube numbers.
- Pages 25/26. **Prime Numbers 2.**  
Finding Prime Factors and leaving in index notation. Finding Highest Common

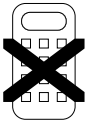
- Factors. An exercise using common factors to find dimensions of a cuboid. Finally finding Lowest Common Multiples.
- Page 27. **Factors and Multiples Game.**  
There is a similar game using only the numbers 1- 25, but it doesn't have a solution. This puzzle has been changed so pupil's don't feel cheated and can find a solution!
- Pages 28/29. **Investigations using Indices.**  
Investigations using indices.
- Page 30. **Prime Pirate Maze.**  
A very simple way of reinforcing the prime numbers and the "look" of a prime number. With less able groups write on the bottom of the sheet all the prime numbers from 1 to 100 as a reminder. The strategy for solving the maze is interesting to watch. Some pupils start from different points trying to find routes. Some simply colour in the prime numbers at random until the routes appear!
- Page 31. **A Prime Maze.**  
Work out the sum and then follow primes to the exit! Another way of trying to reinforcing prime numbers in an interesting fashion.
- Page 32. **Prime and Square Numbers.**  
A snakes and ladders game used to reinforce prime numbers and square numbers. It makes it a lot more interesting if pupils have to land exactly on the win square to finish.
- Pages 33/34. **Multiplying by Powers of 10.**  
Multiplying by powers of 10 in the format 10, 100, 1000,... as well as in index notation.
- Pages 35/36. **Dividing by Powers of 10.**  
Dividing by powers of 10 in the format 10, 100, 1000,... as well as in index notation.
- Page 37. **Zap to Zero. Place Value.**  
A game using the skills of place value.
- Page 38. **Stamps.**  
Four different investigations using stamps as a central theme.
- Pages 39/40. **Probability (Equally Likely Outcomes).**  
Questions based around equally likely outcomes.
- Pages 41/42. **Assigning Probabilities.**  
The different ways of assigning probabilities are dealt with here. Pupils have to carry out surveys and experiments. There are SAT style questions choosing which method of assigning a probability is best. Finally, comparing Theory and Experimental probabilities.
- Pages 43/44. **Experimental Probabilities.** (Bonus pages).  
Pupils should be encouraged to find probabilities by experiment. Here we have questions based on experiments or surveys that have previously been carried out.

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# Grid Multiplication 1.

This is how you work out  $23 \times 7$  using grid multiplication.

	<b>20</b>	<b>3</b>
<b>7</b>	140	21

$140 + 21 = \underline{161}.$



- A). What sums are being worked out with these grids ?  
You **do not** need to work out the answers !

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- B). Write down the sum being worked out in each grid.  
**Copy the grid and then work out the answer.**

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- C). Draw the appropriate grid and then solve the following problems.



- |                    |                    |                    |                    |                    |
|--------------------|--------------------|--------------------|--------------------|--------------------|
| 1). $4 \times 28$  | 2). $3 \times 62$  | 3). $5 \times 73$  | 4). $7 \times 23$  | 5). $6 \times 35$  |
| 6). $7 \times 45$  | 7). $4 \times 67$  | 8). $8 \times 34$  | 9). $3 \times 95$  | 10). $5 \times 97$ |
| 11). $9 \times 23$ | 12). $3 \times 57$ | 13). $4 \times 93$ | 14). $6 \times 84$ | 15). $7 \times 68$ |
| 16). $8 \times 62$ | 17). $7 \times 97$ | 18). $9 \times 75$ | 19). $6 \times 97$ | 20). $9 \times 87$ |

You can use grid multiplication to work out much harder sums, such as  $36 \times 72$ .

	<b>30</b>	<b>6</b>
<b>70</b>	2100	420
<b>2</b>	60	12

$2100 + 420 + 60 + 12 = \underline{2592}.$



D). What sums are being worked out with these grids ?  
You **do not** need to work out the answers !

1). <b>40</b> <b>1</b>	2). <b>40</b> <b>7</b>	3). <b>80</b> <b>4</b>	4). <b>90</b> <b>8</b>																
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E). Write down the sum being worked out in each grid.  
**Copy the grid and then work out the answer.**

1). <b>30</b> <b>6</b>	2). <b>10</b> <b>7</b>	3). <b>40</b> <b>3</b>	4). <b>30</b> <b>4</b>																
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5). <b>20</b> <b>6</b>	6). <b>10</b> <b>8</b>	7). <b>30</b> <b>3</b>	8). <b>20</b> <b>4</b>																
30 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					20 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					40 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					60 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>				
4 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					4 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					2 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					2 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>				

9). <b>70</b> <b>4</b>	10). <b>40</b> <b>5</b>	11). <b>20</b> <b>9</b>	12). <b>70</b> <b>8</b>																
40 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					30 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					50 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					40 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>				
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13). <b>80</b> <b>3</b>	14). <b>60</b> <b>8</b>	15). <b>70</b> <b>2</b>	16). <b>90</b> <b>4</b>																
20 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					40 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					30 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					50 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>				
6 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					3 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					7 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					1 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>				

17). <b>60</b> <b>2</b>	18). <b>50</b> <b>1</b>	19). <b>30</b> <b>9</b>	20). <b>90</b> <b>5</b>																
70 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					80 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					70 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					20 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>				
6 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					3 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					2 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>					9 <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td> </td><td> </td></tr><tr><td> </td><td> </td></tr></table>				

F). Draw the appropriate grid and then solve the following problems.

- |              |              |              |              |              |
|--------------|--------------|--------------|--------------|--------------|
| 1). 34 x 64  | 2). 57 x 63  | 3). 38 x 54  | 4). 93 x 18  | 5). 41 x 32  |
| 6). 53 x 36  | 7). 63 x 39  | 8). 72 x 48  | 9). 19 x 74  | 10). 38 x 92 |
| 11). 69 x 48 | 12). 74 x 38 | 13). 63 x 85 | 14). 78 x 69 | 15). 85 x 59 |
| 16). 97 x 84 | 17). 76 x 85 | 18). 49 x 98 | 19). 96 x 87 | 20). 79 x 86 |





## Grid Multiplication 2.



A). These multiplication grids have been partly filled in.  
Copy each one and fill in the missing numbers.

- 1). 

<b>30</b>	<b>2</b>
	12

      2). 

<b>50</b>	<b>3</b>
	12

      3). 

<b>70</b>	<b>70</b>
140	12

      4). 

<b>5</b>	<b>5</b>
200	35
- = 192**      **= 212**      **= 152**      **= 235**
- 5). 

<b>5</b>	<b>5</b>
180	15

      6). 

<b>20</b>	<b>20</b>
140	28

      7). 

<b>4</b>	<b>4</b>
240	28

      8). 

<b>90</b>	<b>6</b>
	18
- = \_\_\_**      **= \_\_\_**      **= \_\_\_**      **= \_\_\_**
- 9). 

<b>6</b>	<b>6</b>
300	

      10). 

<b>9</b>	<b>9</b>
	36

      11). 

<b>6</b>	<b>6</b>
	42

      12). 

<b>8</b>	<b>8</b>
240	
- = 324**      **= 356**      **= 392**      **= 280**
- 13). 

<b>60</b>	<b>4</b>
540	

      14). 

<b>6</b>	<b>6</b>
420	12

      15). 

<b>8</b>	<b>8</b>
	32

      16). 

<b>80</b>	<b>80</b>
	45
- = \_\_\_**      **= \_\_\_**      **= 392**      **= 445**
- 17). 

<b>60</b>	<b>60</b>
21	

      18). 

<b>100</b>	<b>100</b>
35	

      19). 

<b>150</b>	<b>150</b>
45	

      20). 

<b>180</b>	<b>180</b>
27	
- = \_\_\_**      **= \_\_\_**      **= \_\_\_**      **= \_\_\_**
- 21). 

<b>280</b>	<b>280</b>
21	

      22). 

<b>200</b>	<b>200</b>
16	

      23). 

<b>150</b>	<b>150</b>
12	

      24). 

<b>200</b>	<b>200</b>
8	
- = \_\_\_**      **= \_\_\_**      **= \_\_\_**      **= \_\_\_**
- 25). 

<b>240</b>	<b>240</b>
18	

      26). 

<b>400</b>	<b>400</b>
24	

      27). 

<b>420</b>	<b>420</b>
36	

      28). 

<b>540</b>	<b>540</b>
36	
- = \_\_\_**      **= \_\_\_**      **= \_\_\_**      **= \_\_\_**
- 29). 

<b>450</b>	
------------	--

      30). 

<b>280</b>	
------------	--

      31). 

	40
--	----

      32). 

	36
--	----
- = 470**      **= 336**      **= 760**      **= 516**
- 33). 

<b>720</b>	
------------	--

      34). 

	28
--	----

      35). 

	72
--	----

      36). 

<b>810</b>	
------------	--
- = 783**      **= 588**      **= 632**      **= 846**

B). These are harder multiplication grids. They also have been partly filled in. Copy each one and fill in the missing numbers.



1).

<b>30</b>	600	
<b>2</b>		10

= 800

2).

<b>30</b>	<b>7</b>
1200	
	21

= \_\_\_

3).

<b>50</b>	<b>4</b>
1000	
	4

= \_\_\_

4).

<b>60</b>	
1800	
<b>4</b>	12

= \_\_\_

5).

<b>50</b>	<b>2</b>
2000	
	14

= \_\_\_

6).

<b>3</b>	
	180
<b>2</b>	80

= \_\_\_

7).

<b>20</b>	
<b>50</b>	450
140	

= \_\_\_

8).

<b>60</b>	
1200	
<b>8</b>	56

= \_\_\_

9).

600	100
120	20

= 840

10).

1200	240
60	12

= 1512

11).

2400	420
80	14

= 2914

12).

1400	80
630	36

= 2146

13).

3000	360
100	12

= 3472

14).

2100	420
120	24

= 2664

15).

2000	300
80	12

= \_\_\_

16).

2400	420
40	7

= \_\_\_

17).

600	140
270	63

= \_\_\_

18).

900	210
120	28

= \_\_\_

19).

3500	50
560	8

= \_\_\_

20).

2000	450
280	63

= \_\_\_

21).

600	60
180	

= 858

22).

600	120
	18

= 828

23).

	120
630	36

= 2886

24).

4200	
180	15

= 4745

25).

5600	210
560	

= 6391

26).

5400	
450	5

= 5915

27).

4800	320
	28

= 5568

28).

	180
210	6

= 6696



## Long Multiplications.



Copy and answer the following questions.

### Multiplications.



1).  $\begin{array}{r} 24 \\ \underline{4} \times \end{array}$     2).  $\begin{array}{r} 56 \\ \underline{5} \times \end{array}$     3).  $\begin{array}{r} 72 \\ \underline{8} \times \end{array}$     4).  $\begin{array}{r} 45 \\ \underline{9} \times \end{array}$     5).  $\begin{array}{r} 95 \\ \underline{3} \times \end{array}$

6).  $47 \times 6$     7).  $78 \times 4$     8).  $96 \times 6$     9).  $73 \times 5$     10).  $81 \times 8$   
11).  $36 \times 9$     12).  $53 \times 7$     13).  $28 \times 8$     14).  $39 \times 9$     15).  $97 \times 6$

16).  $\begin{array}{r} 517 \\ \underline{5} \times \end{array}$     17).  $\begin{array}{r} 409 \\ \underline{6} \times \end{array}$     18).  $\begin{array}{r} 624 \\ \underline{4} \times \end{array}$     19).  $\begin{array}{r} 536 \\ \underline{3} \times \end{array}$     20).  $\begin{array}{r} 246 \\ \underline{7} \times \end{array}$

21).  $583 \times 4$     22).  $603 \times 6$     23).  $704 \times 5$     24).  $389 \times 7$     25).  $639 \times 8$   
26).  $419 \times 8$     27).  $874 \times 7$     28).  $892 \times 9$     29).  $486 \times 7$     30).  $793 \times 9$

31).  $\begin{array}{r} 2552 \\ \underline{3} \times \end{array}$     32).  $\begin{array}{r} 6406 \\ \underline{5} \times \end{array}$     33).  $\begin{array}{r} 6437 \\ \underline{4} \times \end{array}$     34).  $\begin{array}{r} 3379 \\ \underline{6} \times \end{array}$     35).  $\begin{array}{r} 2394 \\ \underline{7} \times \end{array}$

36).  $4605 \times 7$     37).  $8930 \times 6$     38).  $1438 \times 7$     39).  $4582 \times 5$     40).  $9403 \times 6$   
41).  $3742 \times 8$     42).  $8462 \times 7$     43).  $7932 \times 9$     44).  $2573 \times 6$     45).  $9607 \times 9$

### Long Multiplications.

1).  $\begin{array}{r} 32 \\ \underline{21} \times \\ \hline \\ \hline \end{array}$     2).  $\begin{array}{r} 43 \\ \underline{52} \times \\ \hline \\ \hline \end{array}$     3).  $\begin{array}{r} 49 \\ \underline{25} \times \\ \hline \\ \hline \end{array}$     4).  $\begin{array}{r} 63 \\ \underline{32} \times \\ \hline \\ \hline \end{array}$     5).  $\begin{array}{r} 53 \\ \underline{45} \times \\ \hline \\ \hline \end{array}$

6).  $\begin{array}{r} 53 \\ \underline{46} \times \\ \hline \\ \hline \end{array}$     7).  $\begin{array}{r} 64 \\ \underline{28} \times \\ \hline \\ \hline \end{array}$     8).  $\begin{array}{r} 39 \\ \underline{28} \times \\ \hline \\ \hline \end{array}$     9).  $\begin{array}{r} 48 \\ \underline{39} \times \\ \hline \\ \hline \end{array}$     10).  $\begin{array}{r} 83 \\ \underline{25} \times \\ \hline \\ \hline \end{array}$

11).  $\begin{array}{r} 59 \\ \underline{56} \times \\ \hline \\ \hline \end{array}$     12).  $\begin{array}{r} 65 \\ \underline{82} \times \\ \hline \\ \hline \end{array}$     13).  $\begin{array}{r} 25 \\ \underline{79} \times \\ \hline \\ \hline \end{array}$     14).  $\begin{array}{r} 75 \\ \underline{47} \times \\ \hline \\ \hline \end{array}$     15).  $\begin{array}{r} 93 \\ \underline{43} \times \\ \hline \\ \hline \end{array}$

16).  $\begin{array}{r} 49 \\ \underline{86} \times \\ \hline \\ \hline \end{array}$     17).  $\begin{array}{r} 67 \\ \underline{92} \times \\ \hline \\ \hline \end{array}$     18).  $\begin{array}{r} 47 \\ \underline{81} \times \\ \hline \\ \hline \end{array}$     19).  $\begin{array}{r} 84 \\ \underline{93} \times \\ \hline \\ \hline \end{array}$     20).  $\begin{array}{r} 97 \\ \underline{86} \times \\ \hline \\ \hline \end{array}$

21).  $34 \times 78$     22).  $76 \times 76$     23).  $29 \times 75$     24).  $56 \times 83$     25).  $67 \times 85$   
26).  $48 \times 76$     27).  $72 \times 91$     28).  $89 \times 97$     29).  $48 \times 86$     30).  $98 \times 99$





### Even Longer Multiplications !

1).  $\begin{array}{r} 324 \\ \underline{14} \times \\ \hline \hline \end{array}$       2).  $\begin{array}{r} 251 \\ \underline{23} \times \\ \hline \hline \end{array}$       3).  $\begin{array}{r} 405 \\ \underline{17} \times \\ \hline \hline \end{array}$       4).  $\begin{array}{r} 721 \\ \underline{32} \times \\ \hline \hline \end{array}$       5).  $\begin{array}{r} 373 \\ \underline{43} \times \\ \hline \hline \end{array}$

6).  $\begin{array}{r} 527 \\ \underline{36} \times \\ \hline \hline \end{array}$       7).  $\begin{array}{r} 409 \\ \underline{41} \times \\ \hline \hline \end{array}$       8).  $\begin{array}{r} 724 \\ \underline{26} \times \\ \hline \hline \end{array}$       9).  $\begin{array}{r} 936 \\ \underline{27} \times \\ \hline \hline \end{array}$       10).  $\begin{array}{r} 646 \\ \underline{35} \times \\ \hline \hline \end{array}$

11).  $\begin{array}{r} 952 \\ \underline{58} \times \\ \hline \hline \end{array}$       12).  $\begin{array}{r} 846 \\ \underline{82} \times \\ \hline \hline \end{array}$       13).  $\begin{array}{r} 637 \\ \underline{75} \times \\ \hline \hline \end{array}$       14).  $\begin{array}{r} 379 \\ \underline{48} \times \\ \hline \hline \end{array}$       15).  $\begin{array}{r} 294 \\ \underline{86} \times \\ \hline \hline \end{array}$

16).  $\begin{array}{r} 684 \\ \underline{96} \times \\ \hline \hline \end{array}$       17).  $\begin{array}{r} 973 \\ \underline{78} \times \\ \hline \hline \end{array}$       18).  $\begin{array}{r} 749 \\ \underline{93} \times \\ \hline \hline \end{array}$       19).  $\begin{array}{r} 869 \\ \underline{78} \times \\ \hline \hline \end{array}$       20).  $\begin{array}{r} 958 \\ \underline{68} \times \\ \hline \hline \end{array}$

21).  $\begin{array}{r} 903 \\ \underline{53} \times \\ \hline \hline \end{array}$       22).  $\begin{array}{r} 486 \\ \underline{65} \times \\ \hline \hline \end{array}$       23).  $\begin{array}{r} 672 \\ \underline{38} \times \\ \hline \hline \end{array}$       24).  $\begin{array}{r} 948 \\ \underline{99} \times \\ \hline \hline \end{array}$       25).  $\begin{array}{r} 683 \\ \underline{65} \times \\ \hline \hline \end{array}$

26).  $\begin{array}{r} 759 \\ \underline{56} \times \\ \hline \hline \end{array}$       27).  $\begin{array}{r} 605 \\ \underline{87} \times \\ \hline \hline \end{array}$       28).  $\begin{array}{r} 925 \\ \underline{89} \times \\ \hline \hline \end{array}$       29).  $\begin{array}{r} 975 \\ \underline{67} \times \\ \hline \hline \end{array}$       30).  $\begin{array}{r} 793 \\ \underline{73} \times \\ \hline \hline \end{array}$

31).  $804 \times 67$     32).  $487 \times 62$     33).  $839 \times 84$     34).  $942 \times 58$     35).  $507 \times 82$   
36).  $983 \times 38$     37).  $843 \times 79$     38).  $399 \times 78$     39).  $287 \times 56$     40).  $989 \times 76$

### Harder Questions

41).  $\begin{array}{r} 6532 \\ \underline{24} \times \\ \hline \hline \end{array}$       42).  $\begin{array}{r} 1425 \\ \underline{37} \times \\ \hline \hline \end{array}$       43).  $\begin{array}{r} 7826 \\ \underline{63} \times \\ \hline \hline \end{array}$       44).  $\begin{array}{r} 7964 \\ \underline{86} \times \\ \hline \hline \end{array}$       45).  $\begin{array}{r} 9361 \\ \underline{74} \times \\ \hline \hline \end{array}$



46).  $\begin{array}{r} 5473 \\ \underline{431} \times \\ \hline \hline \end{array}$       47).  $\begin{array}{r} 2544 \\ \underline{253} \times \\ \hline \hline \end{array}$       48).  $\begin{array}{r} 6036 \\ \underline{147} \times \\ \hline \hline \end{array}$       49).  $\begin{array}{r} 8697 \\ \underline{657} \times \\ \hline \hline \end{array}$       50).  $\begin{array}{r} 4621 \\ \underline{365} \times \\ \hline \hline \end{array}$

51).  $\begin{array}{r} 2483 \\ \underline{632} \times \\ \hline \hline \end{array}$       52).  $\begin{array}{r} 7583 \\ \underline{672} \times \\ \hline \hline \end{array}$       53).  $\begin{array}{r} 9376 \\ \underline{976} \times \\ \hline \hline \end{array}$       54).  $\begin{array}{r} 8793 \\ \underline{796} \times \\ \hline \hline \end{array}$       55).  $\begin{array}{r} 2964 \\ \underline{573} \times \\ \hline \hline \end{array}$





## Division.



Copy and solve the following questions.

1).  $4 \overline{) 92}$  2).  $6 \overline{) 84}$  3).  $3 \overline{) 93}$  4).  $5 \overline{) 80}$

5).  $8 \overline{) 96}$  6).  $4 \overline{) 76}$  7).  $7 \overline{) 98}$  8).  $6 \overline{) 90}$

9).  $81 \div 3$  10).  $96 \div 6$  11).  $90 \div 5$  12).  $72 \div 4$

13).  $5 \overline{) 820}$  14).  $4 \overline{) 852}$  15).  $3 \overline{) 618}$  16).  $9 \overline{) 936}$

17).  $6 \overline{) 642}$  18).  $3 \overline{) 948}$  19).  $7 \overline{) 980}$  20).  $4 \overline{) 948}$

21).  $892 \div 4$  22).  $627 \div 3$  23).  $984 \div 4$  24).  $980 \div 5$

25).  $848 \div 8$  26).  $882 \div 6$  27).  $963 \div 9$  28).  $763 \div 7$

29).  $3 \overline{) 7023}$  30).  $5 \overline{) 8420}$  31).  $6 \overline{) 6336}$  32).  $8 \overline{) 8784}$

33).  $7 \overline{) 9506}$  34).  $9 \overline{) 9072}$  35).  $6 \overline{) 8808}$  36).  $8 \overline{) 9984}$

37).  $9530 \div 5$  38).  $7476 \div 7$  39).  $9981 \div 9$  40).  $8472 \div 12$

41).  $7896 \div 8$  42).  $9482 \div 11$  43).  $6276 \div 12$  44).  $6120 \div 6$

45).  $5 \overline{) 81755}$  46).  $4 \overline{) 92268}$  47).  $6 \overline{) 66582}$  48).  $3 \overline{) 89619}$

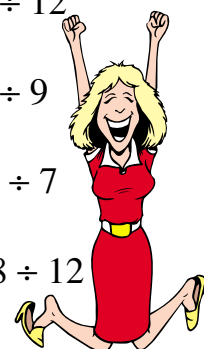
49).  $7 \overline{) 83020}$  50).  $9 \overline{) 97254}$  51).  $8 \overline{) 96448}$  52).  $7 \overline{) 84028}$

53).  $81252 \div 6$  54).  $76012 \div 4$  55).  $86886 \div 9$  56).  $72048 \div 12$

57).  $91014 \div 7$  58).  $61854 \div 6$  59).  $78912 \div 8$  60).  $80154 \div 9$

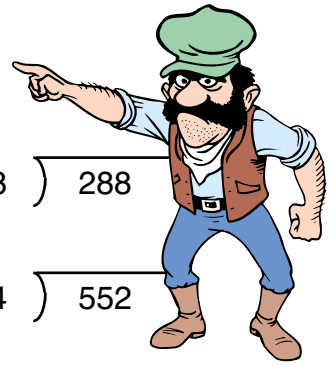
61).  $196224 \div 3$  62).  $118240 \div 5$  63).  $281238 \div 6$  64).  $670894 \div 7$

65).  $325332 \div 9$  66).  $665301 \div 7$  67).  $725648 \div 8$  68).  $1180248 \div 12$

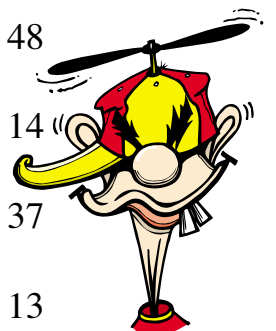




## Long Division.

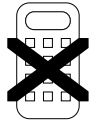


- 1).  $12 \overline{) 276}$     2).  $13 \overline{) 416}$     3).  $12 \overline{) 420}$     4).  $18 \overline{) 288}$
- 5).  $15 \overline{) 270}$     6).  $21 \overline{) 336}$     7).  $19 \overline{) 456}$     8).  $24 \overline{) 552}$
- 9).  $12 \overline{) 228}$     10).  $17 \overline{) 221}$     11).  $13 \overline{) 312}$     12).  $14 \overline{) 182}$
- 13).  $15 \overline{) 345}$     14).  $16 \overline{) 416}$     15).  $14 \overline{) 350}$     16).  $19 \overline{) 437}$
- 17).  $18 \overline{) 612}$     18).  $23 \overline{) 782}$     19).  $17 \overline{) 714}$     20).  $28 \overline{) 728}$
- 21).  $17 \overline{) 442}$     22).  $23 \overline{) 943}$     23).  $26 \overline{) 806}$     24).  $32 \overline{) 768}$
- 25).  $33 \overline{) 858}$     26).  $25 \overline{) 475}$     27).  $32 \overline{) 448}$     28).  $31 \overline{) 527}$
- 29).  $44 \overline{) 924}$     30).  $26 \overline{) 910}$     31).  $33 \overline{) 924}$     32).  $52 \overline{) 936}$
- 33).  $41 \overline{) 984}$     34).  $29 \overline{) 899}$     35).  $36 \overline{) 972}$     36).  $27 \overline{) 702}$
- 37).  $62 \overline{) 806}$     38).  $71 \overline{) 852}$     39).  $54 \overline{) 810}$     40).  $83 \overline{) 996}$
- 41).  $882 \div 42$     42).  $936 \div 39$     43).  $784 \div 56$     44).  $979 \div 89$
- 45).  $841 \div 29$     46).  $833 \div 17$     47).  $874 \div 46$     48).  $962 \div 37$
- 49).  $936 \div 72$     50).  $864 \div 24$     51).  $891 \div 33$     52).  $848 \div 16$
- 53).  $938 \div 67$     54).  $672 \div 42$     55).  $754 \div 58$     56).  $912 \div 48$
- 57).  $925 \div 37$     58).  $448 \div 28$     59).  $784 \div 16$     60).  $826 \div 14$
- 61).  $884 \div 26$     62).  $935 \div 85$     63).  $966 \div 46$     64).  $666 \div 37$
- 65).  $770 \div 55$     66).  $782 \div 46$     67).  $980 \div 49$     68).  $663 \div 13$





## Long Multiplication and Division Problems.



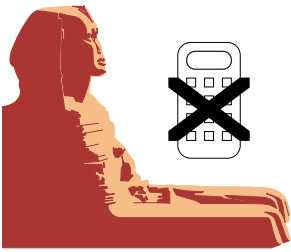
- 1). Bottles of Lemonade are 64 p each. John needs 18 for a party. How much does he spend ?
- 2). There are 864 pupils and staff in a school. They all go to visit London on a school trip. How many 36 seat coaches do they need to hire ?
- 3). Drawing pins come in boxes of 48. The Mathematics Department orders 17 boxes, how many drawing pins have they ordered ?
- 4). A train carriage can hold 118 people. If a train has 14 carriages, how many people can it transport ?
- 5). A roadside florist sells only tulips. They cost 32p each. He takes £ 8.96 at the end of the day. How many tulips has he sold ?
- 6). Mandy the model maker is building a tank out of matches. Matches come in boxes of 52. She works out she needs 832 matches. How many boxes does she need to buy ?
- 7). Bobby thinks there is a Salad Cream shortage and goes shopping. Salad Cream comes in bottles weighing 285 g. He buys 42. How heavy is all the Salad Cream in grams ?
- 8). Jenny has a catering pack of tomato ketchup. It has 882 ml in it. Her job is to put it into tiny 18 ml sachets. How many sachets can she fill ?
- 9). Milk is carried in crates which hold 24 bottles. A milk man sets off on his round with 142 full crates, all for delivery. How many bottles of milk is he delivering ?
- 10). Gemma is holding a Garden Party. She needs 6149 biscuits. A packet holds 43 biscuits.
  - a). How many packets must she buy ?
  - b). One packet costs 97p. How much is she going to spend on biscuits ?
- 11). Laura holds a raffle to raise money for local charities. She sells 36 tickets at £ 4.75 each.
  - a). How much does she raise ?
  - b). The money is to be shared equally between 25 charities. How much will each get ?
- 12). The new intake in a large school is 468. They are to be put into classes of 26 pupils each.
  - a). How many classes are there to be ?
  - b). Each pupil from the new intake pays 54p towards the School Fund. How much will the new intake contribute to the School Fund ?
- 13). The 36 workers from a chocolate factory go on a staff outing. The owner gives them 972 bars of chocolate for the journey.
  - a). How many bars of chocolate do they get each ?
  - b). Unfortunately it is a bumpy journey and everyone is sick! The coach driver charges them £ 88.20 to clear up the mess. How much do they each have to pay ?
- 14). A train holds 342 people. Each person paid £37 for a ticket.
  - a). How much was paid in total for the tickets?
  - b). The train company works out that on average each customer pays 87p for food from the Buffet Trolley. How much would the Buffet Trolley take on this journey ?



## Real Life Problems.

- 1). Bottles of Cola are 44 p each. John needs as many as he can get. He has £6.50.
  - a). How many can he buy ?
  - b). How much change would he get back ?
- 2). There are 900 pupils and staff in a school. They all go to visit London on a school trip.
  - a). How many 42 seat coaches do they need to hire ?
  - b). How many spare seats will there be ?
- 3). Paperclips come in boxes of 52. The Mathematics Department needs 800 paperclips ?
  - a). How many boxes do they need to buy?
  - b). How many spare paperclips will there be ?
- 4). A train has 15 carriages, each carriage can hold up to 68 people. Bury F.C. wishes to take 905 football supporters to an away match.
  - a). Will there be enough room on the train ? (Show working out).
  - b). Calculate how too many/few seats there are?
- 5). A roadside florist sells only roses. They cost 28p each.
  - a). A man asks for £5 worth. How many roses will he get ?
  - b). How much change will he get ?
- 6). Fiona the model maker is building a ship out of matches. Matches come in boxes of 47. She works out she needs 980 matches.
  - a). How many boxes does she need to buy ?
  - b). How many spare matches will she have ?
  - c). Each box of matches costs 36p. How much will Fiona spend on matches ?
- 7). Sarah has a catering pack of Salad Cream. It has 740 ml in it. Her job is to put it into tiny 23 ml sachets.
  - a). How many sachets can she fill ?
  - b). How much will she have left over ?
  - c). The sachets are to be charged at 18p each. How much will she get for all the full sachets?
- 8). Hazel is holding a Garden Party. She needs 4000 biscuits. A packet holds 36 biscuits.
  - a). How many packets must she buy ?
  - b). How many extra biscuits will she have left ?
  - c). One packet costs 54p. How much is she going to spend on biscuits ?
- 9). The new intake in a large school is 370. They are to be put into classes of 28 pupils each.
  - a). How many classes are there to be ?
  - b). If all the classes except the last one have 28 pupils in, how many will the last class have in it ?
  - c). Each pupil from the new intake pays £1.25 towards the School Fund. How much will the new intake contribute to the School Fund ?
- 10). A train can hold 448 people. Each person on the train will pay £68 for a ticket.
  - a). If the train is full, how much did all the tickets cost ?
  - b). The train has 16 carriages, how many people will be in a carriage.
  - c). For this journey there are only 328 passengers
    - i). What is the least number of carriages the train would need ?
    - ii). How many spare seats would there be ?





# Egyptian Multiplication.



Here is a way the Egyptians used to multiply.

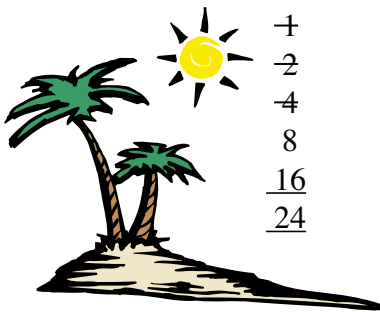
## An easy example.

To solve  $24 \times 33$

Left	Right
1	33
2	66
4	132
8	264
16	528

Write down a left and right column.  
Put 1 in the left column and the bigger number of the sum in the right column.  
Keep doubling both columns.....

until the number in the left column is more than half of the smaller number (24).



Left	Right
1	33
<del>2</del>	<del>66</del>
<del>4</del>	<del>132</del>
8	264
<u>16</u>	<u>528</u> +
<u>24</u>	<u>792</u>

$24 \times 33 = \underline{792}$ .

Now make the smaller number (24) by adding the numbers in the left column. Cross out any we don't need along with those in the right column.  
Add up the numbers that haven't been crossed out in the right column and we have our answer.

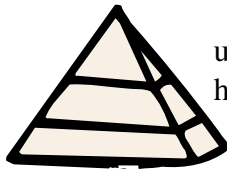
## A Harder Example.

To solve  $43 \times 62$

Left	Right
1	62
2	124
4	248
8	496
16	992
32	1984

Write down a left and right column.  
Put 1 in the left column and the bigger number of the sum in the right column.  
Keep doubling both columns.....

until the number in the left column is more than half of the smaller number (43).



Left	Right
1	62
2	124
<del>4</del>	<del>248</del>
8	496
<del>16</del>	<del>992</del>
<u>32</u>	<u>1984</u> +
<u>43</u>	<u>2666</u>

$43 \times 62 = \underline{2666}$ .

Now make the smaller number (43) by adding the numbers in the left column. Cross out any we don't need along with those in the right column.

Add up the numbers that haven't been crossed out in the right column and we have our answer.

Use this method to solve

- |             |                |     |                |      |                |     |                |
|-------------|----------------|-----|----------------|------|----------------|-----|----------------|
| 1).         | $12 \times 41$ | 2). | $14 \times 32$ | 3).  | $17 \times 68$ | 4). | $24 \times 54$ |
| 5).         | $25 \times 35$ | 6). | $34 \times 46$ | 7).  | $41 \times 53$ | 8). | $45 \times 61$ |
| <b>Hard</b> |                | 9). | $29 \times 34$ | 10). | $55 \times 72$ |     |                |





# Russian Multiplication.



Here is a way the Russians used to multiply.

## An easy example.

To solve  $45 \times 67$

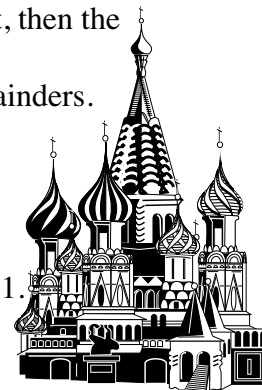
Small No.	Big No.
45	67
22	134
11	268
5	536
2	1072
1	2144

Small No.	Big No.
45	67
<del>22</del>	<del>134</del>
11	268
5	536
<del>2</del>	<del>1072</del>
1	<u>2144</u>
	<u>3015</u>

$45 \times 67 = \underline{3015}$ .

Write down the smaller number first, then the bigger number.  
Halve the small number-ignore remainders.  
Double the big number column.

Stop when the small numbers reach 1.



Look in the small number column and cross out any numbers that are even numbers. Cross out the number on the same level in the Big number column.

Add up the numbers that haven't been crossed out in the big number column and we have our answer.

## A Harder Example.

To solve  $216 \times 73$

Small No.	Big No.
73	216
36	432
18	864
9	1728
4	3456
2	6912
1	13824

Small No.	Big No.
73	216
<del>36</del>	<del>432</del>
<del>18</del>	<del>864</del>
9	1728
4	3456
2	6912
1	<u>13824</u>
	<u>15768</u>

$216 \times 73 = \underline{15768}$ .

Write down the smaller number first, then the bigger number.  
Halve the small number-ignore remainders.  
Double the big number column.

Stop when the small numbers reach 1.

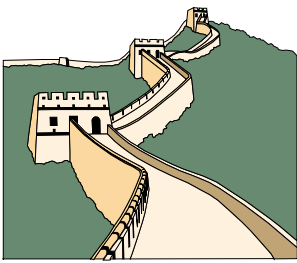
Look in the small number column and cross out any numbers that are even numbers. Cross out the number on the same level in the Big number column.

Add up the numbers that haven't been crossed out in the big number column and we have our answer.

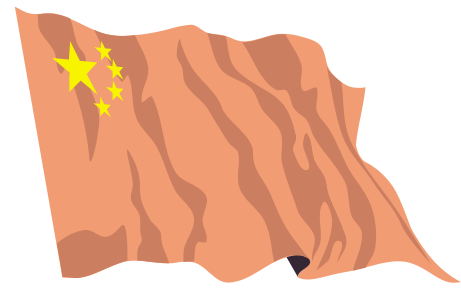


Use this method to solve

- |                    |                     |                      |                    |
|--------------------|---------------------|----------------------|--------------------|
| 1). $24 \times 36$ | 2). $19 \times 53$  | 3). $39 \times 33$   | 4). $57 \times 42$ |
| 5). $37 \times 78$ | 6). $36 \times 67$  | 7). $41 \times 53$   | 8). $82 \times 54$ |
| <b>Hard</b>        | 9). $29 \times 134$ | 10). $85 \times 172$ |                    |



# Chinese Multiplication.

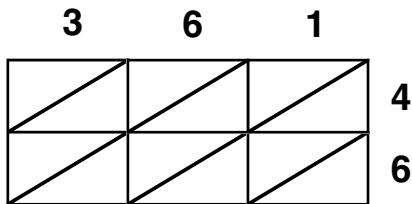


Here is a way the Chinese used to multiply.

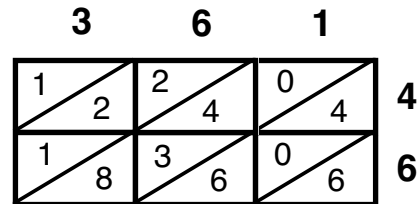
An easy example.

Solve  $361 \times 46$ .

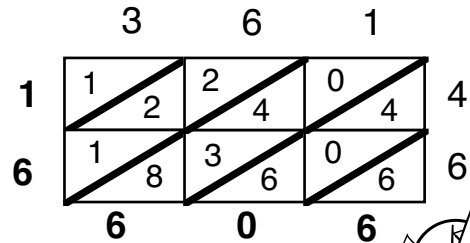
- A). Write the numbers along the top and down the right hand side of a rectangular grid as shown.



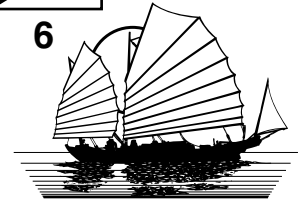
- B). Each pair is multiplied out and the answer put in the relevant box. The tens in the top half and units in the bottom half.



- C). The numbers are added up diagonally, starting just with the 6. The next is  $4 + 0 + 6 = 10$ . The 0 is put down and the 1 carried to the next diagonal to be added up.



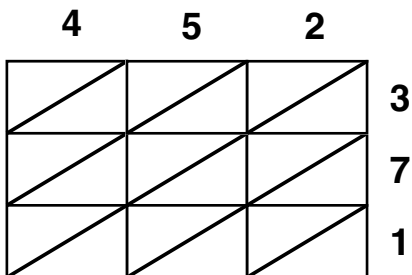
- D). This is now read from the 1.  $361 \times 46 = 16606$ .



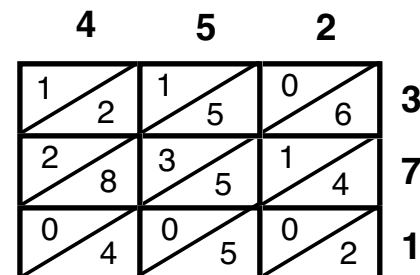
A hard example.

Solve  $452 \times 371$ .

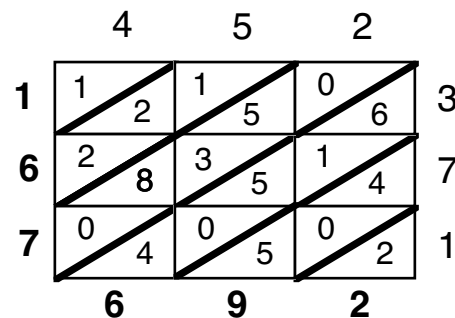
- A). Write the numbers along the top and down the right hand side of a rectangular grid as shown.



- B). Each pair is multiplied out and the answer put in the relevant box.



- C). The numbers are added up diagonally, starting in the bottom right corner. Remember to carry.

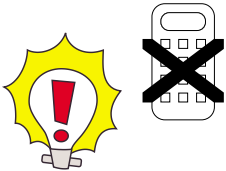


- D). Read off the answer.

$452 \times 371 = 167692$ .

Try answering these using this method.

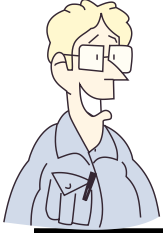
- |                     |                      |                       |                     |
|---------------------|----------------------|-----------------------|---------------------|
| 1). $361 \times 46$ | 2). $264 \times 54$  | 3). $648 \times 49$   | 4). $518 \times 73$ |
| 5). $327 \times 98$ | 6). $676 \times 57$  | 7). $941 \times 83$   | 8). $892 \times 74$ |
| <b>Hard</b>         | 9). $219 \times 134$ | 10). $835 \times 472$ |                     |



# Spiralling Sums 1 (Long Multiplication).



Work out and then write in the answers to the following:



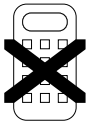
- |                             |                              |                              |
|-----------------------------|------------------------------|------------------------------|
| 1). $16 \times 23 =$ _____  | 2). $16 \times 51 =$ _____   | 3). $58 \times 42 =$ _____   |
| 4). $73 \times 36 =$ _____  | 5). $94 \times 57 =$ _____   | 6). $39 \times 16 =$ _____   |
| 7). $69 \times 45 =$ _____  | 8). $34 \times 29 =$ _____   | 9). $97 \times 86 =$ _____   |
| 10). $48 \times 19 =$ _____ | 11). $124 \times 43 =$ _____ | 12). $215 \times 29 =$ _____ |



- 13). Start at the centre of the spiral and write out the answers in words in the appropriate places.
- 14). Hidden in the spiral are **three** mystery countries. To find the countries read off the letters in the shaded squares starting at the centre of the spiral.





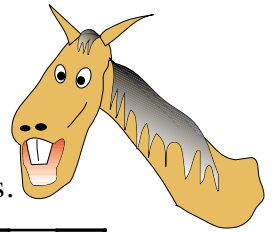


# The Number Six Multiple Maze.

Zeb has lost her stripes. She has to get through the maze to find them.

She can only travel along **multiples of 6**.

Work out each sum. Now find the route she must take to find her stripes.



IN  $35 + 55 =$   $174 + 54 =$   $212 - 44 =$   $158 + 58 =$   $216 - 66 =$

$112 - 76 =$   $213 - 137 =$   $146 + 74 =$   $171 - 123 =$   $229 - 83 =$   $108 + 222 =$

$78 + 156 =$   $295 - 181 =$   $78 + 48 =$   $314 - 96 =$   $133 + 47 =$

$241 - 157 =$   $87 + 113 =$   $219 - 191 =$   $250 - 64 =$   $333 - 279 =$   $54 + 46 =$

$318 - 260 =$   $97 + 171 =$   $47 + 175 =$   $215 + 137 =$   $400 - 34 =$

$230 - 82 =$   $415 - 343 =$   $128 + 268 =$   $79 + 159 =$   $241 - 155 =$   $97 + 81 =$

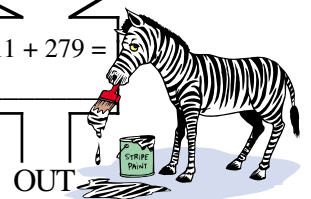
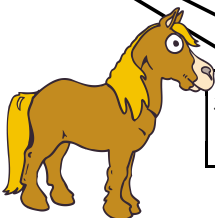
$346 - 226 =$   $163 - 75 =$   $114 + 148 =$   $137 + 115 =$   $68 + 136 =$

$117 + 123 =$   $97 + 243 =$   $175 + 239 =$   $212 - 116 =$   $343 - 233 =$   $249 + 111 =$

$207 + 147 =$   $127 + 179 =$   $420 - 116 =$   $94 + 82 =$   $237 + 183 =$

$421 - 355 =$   $347 - 145 =$   $280 - 168 =$   $64 + 234 =$   $471 - 369 =$   $125 + 177 =$

$532 - 424 =$   $293 + 49 =$   $178 + 68 =$   $517 - 257 =$   $111 + 279 =$



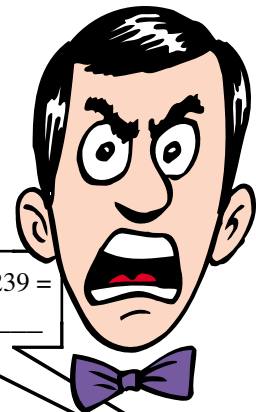
OUT



# The Number Seven Multiple Maze.

Eric has lost his marbles. He has to get through the maze to find them.  
He can only travel along **multiples of 7**.

Work out each sum. Now find the route he must take to regain his sanity!



IN

$124 - 75 =$

$39 + 171 =$

$145 - 75 =$

$237 + 106 =$

$139 + 239 =$

$150 - 24 =$

$119 + 181 =$

$67 + 108 =$

$313 - 63 =$

$217 - 163 =$

$73 + 165 =$

$346 - 253 =$

$106 - 43 =$

$17 + 68 =$

$236 + 114 =$

$400 - 36 =$

$157 + 63 =$

$312 - 67 =$

$431 - 364 =$

$99 + 197 =$

$357 - 222 =$

$59 + 18 =$

$263 - 164 =$

$138 + 268 =$

$138 - 96 =$

$74 + 59 =$

$200 - 58 =$



$79 + 125 =$

$313 - 229 =$

$87 + 83 =$

$143 + 75 =$

$463 - 407 =$

$243 + 117 =$



$64 + 125 =$

$108 + 216 =$

$94 + 74 =$

$300 - 41 =$

$39 + 59 =$

$147 + 77 =$

$59 + 51 =$

$116 + 213 =$

$246 - 95 =$

$346 - 223 =$

$37 + 133 =$

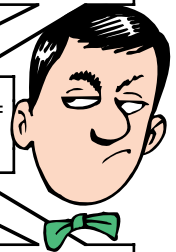
$65 + 117 =$

$421 - 265 =$

$530 - 439 =$

$178 + 74 =$

$139 + 309 =$



$137 + 283 =$

$415 - 149 =$

$109 + 309 =$

$527 - 385 =$

$47 + 91 =$

$65 + 47 =$



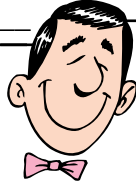
$419 - 372 =$

$521 - 416 =$

$117 + 191 =$

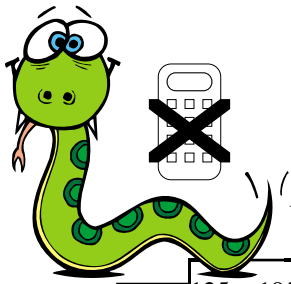
$420 - 243 =$

$279 + 176 =$



OUT



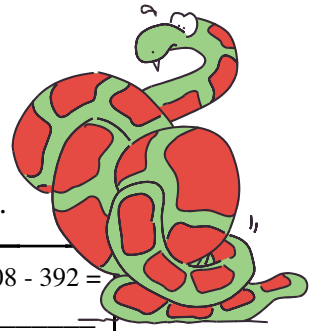


# The Number Eight Multiple Maze.

Sammy has lost his rattle. He has to get through the maze to find it.

He can only travel along **multiples of 8**.

Work out each sum. Now find the route he must take to find his rattle.



IN

$125 + 195 =$

$130 - 58 =$

$65 + 367 =$

$250 - 203 =$

$408 - 392 =$

$211 - 179 =$

$35 + 49 =$

$523 - 488 =$

$97 + 127 =$

$391 - 269 =$

$63 + 177 =$

$282 - 218 =$

$76 + 132 =$

$420 - 50 =$

$38 + 58 =$

$531 - 419 =$

$263 - 183 =$

$54 + 126 =$

$216 + 115 =$

$432 - 392 =$

$200 - 126 =$

$137 + 223 =$

$61 + 67 =$

$240 - 181 =$

$106 + 182 =$

$149 + 295 =$

$42 + 88 =$

$416 - 382 =$

$400 - 168 =$

$74 + 91 =$

$273 - 249 =$

$132 + 284 =$

$613 - 545 =$

$104 + 123 =$

$200 - 22 =$

$147 + 183 =$

$430 - 277 =$

$75 + 45 =$

$472 - 425 =$

$57 + 103 =$

$254 - 206 =$

$124 + 212 =$

$600 - 248 =$

$34 + 245 =$

$550 - 94 =$

$161 - 37 =$

$200 - 8 =$

$234 + 227 =$

$197 - 109 =$

$113 + 153 =$

$347 - 291 =$

$116 + 166 =$

$500 - 39 =$

$637 - 420 =$

$451 - 378 =$

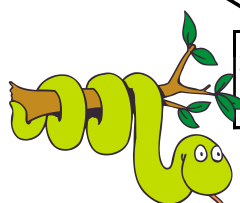
$309 + 117 =$

$49 + 207 =$

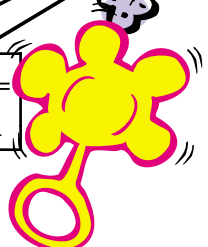
$631 - 431 =$

$242 - 138 =$

$137 + 343 =$



OUT

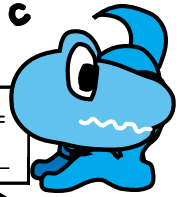
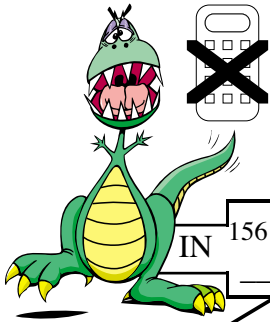


# The Number Nine Multiple Maze.

Dino has lost his saw. He has to get through the maze to find it.

He can only travel along **multiples of 9**.

Work out each sum. Now find the route he must take to find his saw.



IN  $156 + 258 =$   $94 - 76 =$   $31 + 68 =$   $304 - 124 =$   $65 + 88 =$

$428 - 113 =$   $39 + 145 =$   $500 - 206 =$   $214 + 86 =$   $75 + 129 =$   $472 - 238 =$

$112 - 58 =$   $497 - 371 =$   $105 + 174 =$   $365 - 282 =$   $79 + 361 =$

$294 - 213 =$   $605 - 422 =$   $217 + 176 =$   $451 - 262 =$   $81 + 63 =$   $119 + 128 =$

$238 + 158 =$   $420 - 218 =$   $525 - 426 =$   $59 + 177 =$   $532 - 469 =$

$144 + 18 =$   $407 - 323 =$   $177 + 129 =$   $694 - 637 =$   $53 + 217 =$   $204 - 75 =$

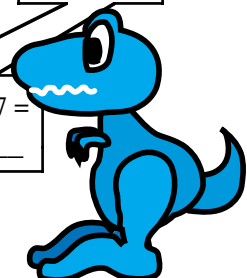
$64 + 156 =$   $613 - 504 =$   $338 - 257 =$   $523 - 486 =$   $416 - 110 =$

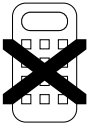
$79 + 106 =$   $167 + 328 =$   $200 - 65 =$   $614 - 379 =$   $48 + 338 =$   $369 + 87 =$

$500 - 248 =$   $65 + 62 =$   $393 - 192 =$   $138 + 159 =$   $637 - 466 =$

$542 - 470 =$   $350 - 265 =$   $108 + 333 =$   $709 - 673 =$   $507 - 187 =$   $370 + 116 =$

$436 - 256 =$   $700 - 376 =$   $79 + 49 =$   $620 - 324 =$   $740 - 407 =$



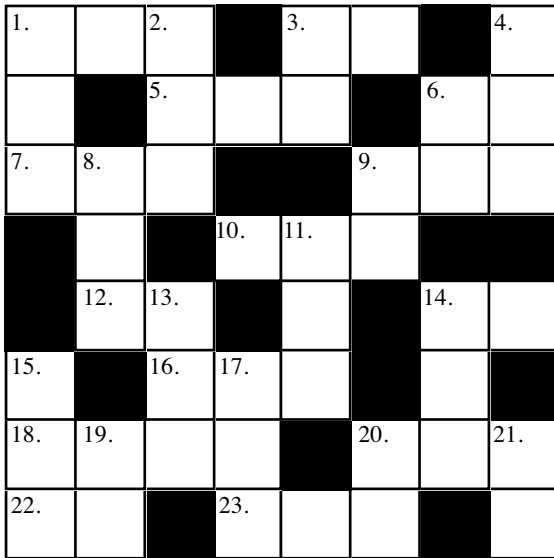


# Multiplication and Division Cross-Numbers.

Work out the answers either in your head or by using a pen and paper method. Put these answers in the cross-number.



A).



### Across.

- |                     |                     |                     |
|---------------------|---------------------|---------------------|
| 1). $16 \times 8$   | 3). $455 \div 13$   | 5). $19 \times 46$  |
| 6). $966 \div 23$   | 7). $18 \times 16$  | 9). $13 \times 37$  |
| 10). $14 \times 16$ | 12). $9 \times 9$   | 14). $603 \div 9$   |
| 16). $68 \times 7$  | 18). $98 \times 29$ | 20). $13 \times 13$ |
| 22). $1056 \div 44$ | 23). $63 \times 14$ |                     |

### Down.

- |                     |                     |                     |
|---------------------|---------------------|---------------------|
| 1). $12 \times 11$  | 2). $37 \times 24$  | 3). $714 \div 21$   |
| 4). $11 \times 11$  | 6). $6 \times 8$    | 8). $36 \times 23$  |
| 9). $748 \div 17$   | 11). $46 \times 6$  | 13). $12 \times 12$ |
| 14). $56 \times 11$ | 15). $14 \times 23$ | 17). $56 \times 13$ |
| 19). $7 \times 12$  | 20). $144 \div 12$  | 21). $665 \div 7$   |

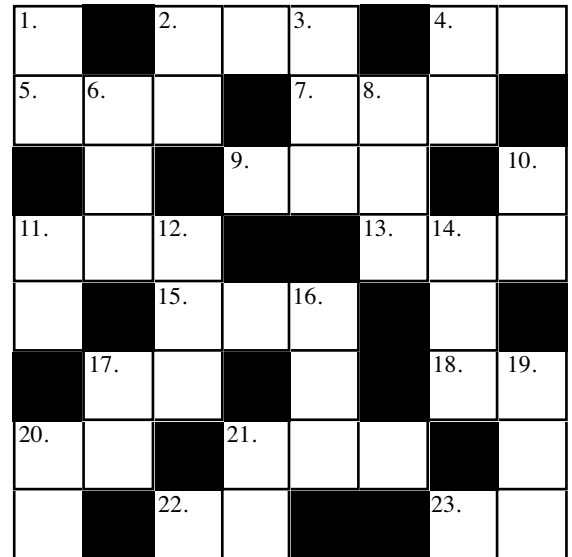
### Across.

- |                     |                     |                     |
|---------------------|---------------------|---------------------|
| 2). $36 \times 21$  | 4). $247 \div 13$   | 5). $13 \times 14$  |
| 7). $24 \times 39$  | 9). $13 \times 13$  | 11). $12 \times 9$  |
| 13). $17 \times 41$ | 15). $94 \times 9$  | 17). $768 \div 32$  |
| 18). $448 \div 7$   | 20). $715 \div 65$  | 21). $25 \times 18$ |
| 22). $969 \div 51$  | 23). $1876 \div 67$ |                     |

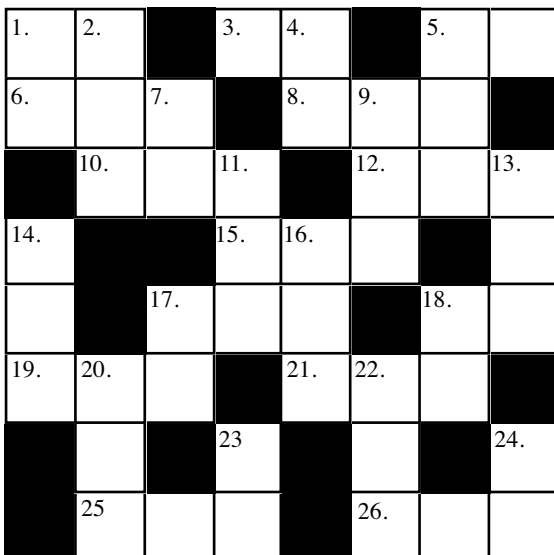
### Down.

- |                     |                     |                     |
|---------------------|---------------------|---------------------|
| 1). $369 \div 9$    | 2). $9 \times 8$    | 3). $87 \times 8$   |
| 4). $128 \div 8$    | 6). $58 \times 15$  | 8). $44 \times 9$   |
| 10). $378 \div 14$  | 11). $910 \div 65$  | 12). $68 \times 13$ |
| 14). $21 \times 46$ | 16). $45 \times 15$ | 17). $252 \div 12$  |
| 19). $6 \times 68$  | 20). $688 \div 43$  | 21). $686 \div 14$  |

B).



C).



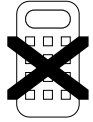
### Across.

- |                     |                     |                     |
|---------------------|---------------------|---------------------|
| 1). $391 \div 23$   | 3). $506 \div 22$   | 5). $230 \div 5$    |
| 6). $68 \times 14$  | 8). $18 \times 18$  | 10). $21 \times 21$ |
| 12). $39 \times 3$  | 15). $47 \times 20$ | 17). $79 \times 11$ |
| 18). $296 \div 8$   | 19). $27 \times 19$ | 21). $13 \times 32$ |
| 25). $16 \times 13$ | 26). $38 \times 18$ |                     |

### Down.

- |                     |                     |                     |
|---------------------|---------------------|---------------------|
| 1). $152 \div 8$    | 2). $29 \times 26$  | 4). $528 \div 16$   |
| 5). $49 \times 9$   | 7). $768 \div 32$   | 9). $15 \times 14$  |
| 11). $14 \times 14$ | 13). $67 \times 11$ | 14). $43 \times 15$ |
| 16). $26 \times 19$ | 17). $581 \div 7$   | 18). $612 \div 17$  |
| 20). $38 \times 4$  | 22). $18 \times 7$  | 23). $950 \div 25$  |
| 24). $504 \div 36$  |                     |                     |

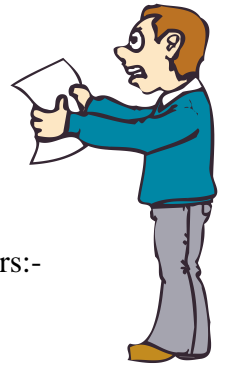
# Prime Numbers 1.



## Multiples.

A). Write out the first six multiples of the following numbers:-

- |         |         |         |         |          |
|---------|---------|---------|---------|----------|
| 1). 4   | 2). 7   | 3). 5   | 4). 3   | 5). 8    |
| 6). 12  | 7). 15  | 8). 9   | 9). 11  | 10). 20  |
| 11). 31 | 12). 45 | 13). 80 | 14). 57 | 15). 123 |



## Factors.

B). Write out the complete set of factors, in ascending order, of the following numbers:-

- |         |         |         |         |          |
|---------|---------|---------|---------|----------|
| 1). 6   | 2). 10  | 3). 5   | 4). 9   | 5). 2    |
| 6). 12  | 7). 1   | 8). 4   | 9). 16  | 10). 20  |
| 11). 8  | 12). 35 | 13). 18 | 14). 24 | 15). 30  |
| 16). 44 | 17). 37 | 18). 52 | 19). 64 | 20). 120 |

Copy the following table, and **complete it up to 30.**



Number	Factors	No. of Factors
1	1	1
2	1,2	2
3	1,3	2
4	1,2,4	3

Which of the following numbers are **prime numbers**.

- C). 1). 18      2). 19      3). 5      4). 9      5). 21  
6). 12      7). 1      8). 3      9). 15      10). 2  
11). 17      12). 33      13). 55      14). 24      15). 35  
16). 31      17). 37      18). 51      19). 64      20). 41  
21). 29      22). 45      23). 59      24). 81      25). 87

## Index Numbers (Powers).

D). We say  $3^5$  as "three to the power five".

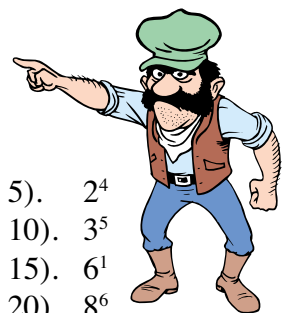
Write out how we say the following :-

- |           |           |           |            |            |
|-----------|-----------|-----------|------------|------------|
| 1). $5^4$ | 2). $8^2$ | 3). $9^4$ | 4). $6^3$  | 5). $2^4$  |
| 6). $6^9$ | 7). $7^6$ | 8). $8^5$ | 9). $12^7$ | 10). $3^5$ |

E).  $3^5$  means  $3 \times 3 \times 3 \times 3 \times 3$

Write out the meanings of the following :-

- |             |            |             |             |            |
|-------------|------------|-------------|-------------|------------|
| 1). $4^5$   | 2). $7^2$  | 3). $5^4$   | 4). $9^3$   | 5). $2^4$  |
| 6). $6^2$   | 7). $4^6$  | 8). $8^3$   | 9). $12^2$  | 10). $3^5$ |
| 11). $8^4$  | 12). $2^7$ | 13). $14^3$ | 14). $10^6$ | 15). $6^1$ |
| 16). $12^5$ | 17). $9^2$ | 18). $20^4$ | 19). $2^1$  | 20). $8^6$ |



F). When a question asks you to **evaluate** it, it means find a value.



Evaluate  $4^2$ .  $4^2$  means  $4 \times 4 = \mathbf{16}$ .

Evaluate the following :-

- |             |             |             |             |            |
|-------------|-------------|-------------|-------------|------------|
| 1). $7^2$   | 2). $3^2$   | 3). $2^3$   | 4). $9^2$   | 5). $2^4$  |
| 6). $6^2$   | 7). $5^3$   | 8). $8^2$   | 9). $12^2$  | 10). $3^3$ |
| 11). $8^3$  | 12). $2^5$  | 13). $11^2$ | 14). $10^3$ | 15). $6^4$ |
| 16). $10^4$ | 17). $9^1$  | 18). $10^6$ | 19). $2^1$  | 20). $5^4$ |
| 21). $7^3$  | 22). $18^1$ | 23). $6^7$  | 24). $9^5$  | 25). $4^7$ |



G). By evaluating the powers, which of these is the bigger number ?

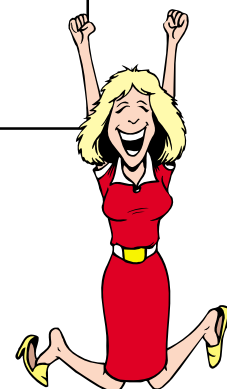
- |                       |                      |                     |                      |
|-----------------------|----------------------|---------------------|----------------------|
| 1). $2^3$ or $5^2$    | 2). $7^2$ or $4^3$   | 3). $3^3$ or $5^2$  | 4). $4^3$ or $6^2$   |
| 5). $2^4$ or $4^2$    | 6). $5^3$ or $10^2$  | 7). $6^3$ or $12^2$ | 8). $8^2$ or $4^3$   |
| 9). $7^3$ or $13^2$   | 10). $8^3$ or $15^2$ | 11). $9^3$ or $5^4$ | 12). $7^4$ or $12^3$ |
| 13). $21^3$ or $10^4$ | 14). $6^4$ or $5^5$  | 15). $7^5$ or $3^8$ | 16). $2^7$ or $4^4$  |
| 17). $3^5$ or $7^3$   | 18). $2^8$ or $4^4$  | 19). $4^5$ or $8^3$ | 20). $6^5$ or $5^6$  |

### Square and Cube Numbers.

H). Numbers that have a power of 2 are called **square** numbers.  $4^2$  is said "4 squared".  
Numbers that have a power of 3 are called **cube** numbers.  $4^3$  is said "4 cubed".

Copy and complete the table up to  $20^2$  and  $20^3$ .

		Square number			Cube number
$1^2$	$1 \times 1$	1	$1^3$	$1 \times 1 \times 1$	1
$2^2$	$2 \times 2$	4	$2^3$	$2 \times 2 \times 2$	8
$3^2$	$3 \times 3$		$3^3$	$3 \times 3 \times 3$	



I). List all the factors of each square number, what do you notice ?  
Why ?

### Square Roots and Cube Roots.

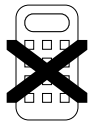
J). The opposite process of squaring a number is **square rooting** a number ( $\sqrt{\quad}$ ).  
Similarly, the opposite process of cubing a number is **cube rooting** a number ( $\sqrt[3]{\quad}$ ).

From your knowledge of squares and cubes, work out the following.

- |                       |                       |                      |                       |                       |
|-----------------------|-----------------------|----------------------|-----------------------|-----------------------|
| 1). $\sqrt{16}$       | 2). $\sqrt{64}$       | 3). $\sqrt[3]{8}$    | 4). $\sqrt[3]{64}$    | 5). $\sqrt{4}$        |
| 6). $\sqrt[3]{27}$    | 7). $\sqrt[3]{1}$     | 8). $\sqrt{1}$       | 9). $\sqrt[3]{125}$   | 10). $\sqrt{100}$     |
| 11). $\sqrt[3]{343}$  | 12). $\sqrt{9}$       | 13). $\sqrt[3]{729}$ | 14). $\sqrt{25}$      | 15). $\sqrt[3]{216}$  |
| 16). $\sqrt{144}$     | 17). $\sqrt{121}$     | 18). $\sqrt[3]{512}$ | 19). $\sqrt{36}$      | 20). $\sqrt{81}$      |
| 21). $\sqrt[3]{1331}$ | 22). $\sqrt{169}$     | 23). $\sqrt{225}$    | 24). $\sqrt[3]{2744}$ | 25). $\sqrt{324}$     |
| 26). $\sqrt{169}$     | 27). $\sqrt[3]{1000}$ | 28). $\sqrt{361}$    | 29). $\sqrt[3]{5832}$ | 30). $\sqrt[3]{8000}$ |



# Prime Numbers 2.



## Prime Factors.

**Reminder. Prime Numbers : 2, 3, 5, 7, 11, 13, 17.....**

This is how we find the prime factors of a number.  
E.g. Find the prime factors of 120.



2	120
	60

Start by finding the smallest prime number that will divide into the number. Divide it!

2	120
2	60
	30

Now find the smallest prime number that will divide into the answer. Divide it!

2	120
2	60
2	30
3	15
5	5
	1

Keep dividing the answers by the smallest prime number. Stop when you reach 1.

Prime factors of 120 are **2 x 2 x 2 x 3 x 5**.

A. Now find the prime factors of these numbers.

- |          |          |          |          |          |
|----------|----------|----------|----------|----------|
| 1). 8    | 2). 10   | 3). 20   | 4). 28   | 5). 36   |
| 6). 24   | 7). 30   | 8). 45   | 9). 40   | 10). 42  |
| 11). 80  | 12). 54  | 13). 64  | 14). 96  | 15). 84  |
| 16). 99  | 17). 81  | 18). 88  | 19). 108 | 20). 112 |
| 21). 168 | 22). 384 | 23). 360 | 24). 216 | 25). 462 |

B. Leave the following in index notation.

e.g.  $2 \times 2 \times 2 \times 5 = 2^3 \times 5$

- |  |  |   |   |
|--|--|---|---|
| 1). $2 \times 3 \times 3$                                      | 2). $2 \times 3 \times 3 \times 5$                             | 3). $2 \times 2 \times 2 \times 5$                    | 4). $2 \times 3 \times 3 \times 3$                    |
| 5). $3 \times 5 \times 5 \times 5$                             | 6). $2 \times 5 \times 5 \times 7$                             | 7). $3 \times 5 \times 5 \times 5$                    | 8). $5 \times 5 \times 5 \times 5 \times 7$           |
| 9). $2 \times 5 \times 7 \times 7 \times 7$                    | 10). $3 \times 5 \times 5 \times 7 \times 7$                   | 11). $5 \times 5 \times 7 \times 7 \times 7$          | 12). $2 \times 2 \times 2 \times 5 \times 7 \times 7$ |
| 13). $2 \times 2 \times 3 \times 3 \times 13$                  | 14). $5 \times 5 \times 7 \times 13 \times 13$                 | 15). $2 \times 5 \times 7 \times 13 \times 13$        | 16). $3 \times 3 \times 3 \times 3 \times 5 \times 5$ |
| 17). $2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 5$ | 18). $2 \times 3 \times 3 \times 5 \times 5 \times 5 \times 5$ | 19). $2 \times 5 \times 7 \times 7 \times 7 \times 7$ | 20). $2 \times 5 \times 5 \times 5 \times 5 \times 5$ |

C. E.g. Find prime factors of 140, leave in index notation.

Prime factors are  $2 \times 2 \times 5 \times 7$   
 $= 2^2 \times 5 \times 7$

2	140
2	70
5	35
7	7
	1

Find the prime factors of the following. **Leave in index notation.**

- |          |          |          |          |          |
|----------|----------|----------|----------|----------|
| 1). 12   | 2). 18   | 3). 16   | 4). 44   | 5). 50   |
| 6). 27   | 7). 25   | 8). 56   | 9). 32   | 10). 75  |
| 11). 72  | 12). 63  | 13). 100 | 14). 180 | 15). 308 |
| 16). 216 | 17). 175 | 18). 288 | 19). 270 | 20). 486 |



D. These numbers have been left in index notation. Find which numbers they are.

- |                       |                              |                                  |                                  |
|-----------------------|------------------------------|----------------------------------|----------------------------------|
| 1). $2^2 \times 5$    | 2). $3^2 \times 7$           | 3). $2^2 \times 13$              | 4). $3^2 \times 5$               |
| 5). $2^2 \times 3^2$  | 6). $2^3 \times 3$           | 7). $2 \times 3^2$               | 8). $2^3 \times 7$               |
| 9). $2 \times 3^3$    | 10). $2^3 \times 3^2$        | 11). $3 \times 5^2$              | 12). $2 \times 7^2$              |
| 13). $3^2 \times 5^2$ | 14). $2 \times 3 \times 5^2$ | 15). $2^2 \times 3^2 \times 7$   | 16). $2^3 \times 7 \times 11$    |
| 17). $3^2 \times 5^3$ | 18). $3 \times 7^2$          | 19). $2^2 \times 3^2 \times 5^2$ | 20). $2^3 \times 3^3 \times 7^2$ |

## Highest Common Factor (H.C.F.).



A. The H.C.F. of two or more numbers is the biggest factor that belongs to all the numbers. One way to find this is to look at the prime factors.

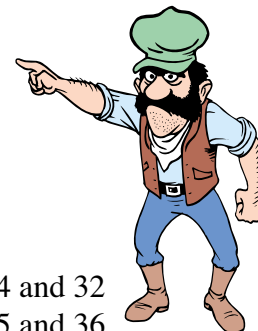
E.g. Find the H.C.F. of 12 and 18.

Prime factors of 12 -  $2 \times 2 \times 3$

These factors belong in both sets.

Prime factors of 18 -  $2 \times 3 \times 3$

The H.C.F is  $2 \times 3 = 6$ .



Find the H.C.F. of the following sets of numbers.

- |                     |                     |                      |                       |
|---------------------|---------------------|----------------------|-----------------------|
| 1). 12 and 18       | 2). 10 and 25       | 3). 14 and 21        | 4). 24 and 32         |
| 5). 30 and 24       | 6). 30 and 45       | 7). 48 and 36        | 8). 45 and 36         |
| 9). 48 and 72       | 10). 42 and 70      | 11). 105 and 63      | 12). 72 and 120       |
| 13). 18, 30 and 42  | 14). 24, 40 and 72  | 15). 27, 18 and 99   | 16). 104, 72 and 56   |
| 17). 36, 96 and 60  | 18). 42, 56 and 98  | 19). 90, 45 and 105  | 20). 36, 63 and 108   |
| 21). 63, 42 and 126 | 22). 108, 54 and 90 | 23). 72, 168 and 120 | 24). 144, 96 and 192. |

B. Here are some cuboids. The areas of each face are given. (The diagrams are not drawn to scale). Work out the length, width and height of each cuboid.

- |      |      |      |      |
|------|------|------|------|
| 1).  | 2).  | 3).  | 4).  |
| 5).  | 6).  | 7).  | 8).  |
| 9).  | 10). | 11). | 12). |
| 13). | 14). | 15). | 16). |

## Lowest Common Multiple (L.C.M.).

The smallest multiple of two or more numbers is called the Lowest Common Multiple (L.C.M.).

E.g. Find the L.C.M. of 4 and 9.

Multiples of 4 : 4, 8, 12, 16, 20, 24, 28, 32, **36**, 40 ....

Multiples of 9 : 9, 18, 27, **36**, 45.....

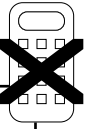
The L.C.M. of 4 and 9 is 36.

Find the Lowest Common multiple of the following sets of numbers.

- |                   |                    |                   |                     |
|-------------------|--------------------|-------------------|---------------------|
| 1). 3 and 4       | 2). 5 and 7        | 3). 6 and 9       | 4). 4 and 7         |
| 5). 8 and 12      | 6). 10 and 15      | 7). 12 and 9      | 8). 10 and 12       |
| 9). 20 and 15     | 10). 12 and 18     | 11). 15 and 25    | 12). 16 and 24      |
| 13). 3, 4 and 5   | 14). 2, 3 and 5    | 15). 3, 4 and 8   | 16). 2, 4 and 9     |
| 17). 5, 8 and 10  | 18). 3, 9 and 12   | 19). 4, 12 and 16 | 20). 8, 12 and 20   |
| 21). 5, 12 and 24 | 22). 15, 20 and 24 | 23). 8, 15 and 20 | 24). 15, 18 and 30. |



# The Factors and Multiples Game



## The Playing Board


Heading Cards

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## Rules.

1. Cut out the Heading Cards and place one in each of the ten spaces around the playing board.

2. Cut out the 25 Number Cards and place each one on the playing board, so it satisfies the condition given by the Heading Cards for each

3. By re-arranging the positions of the Heading Cards and the Number Cards, try to fill in as many squares on the playing board as possible.

## Number Cards

1	2	3	4	5
<u>6</u>	7	8	<u>9</u>	10
11	12	13	14	15
16	17	18	20	21
24	25	27	30	60

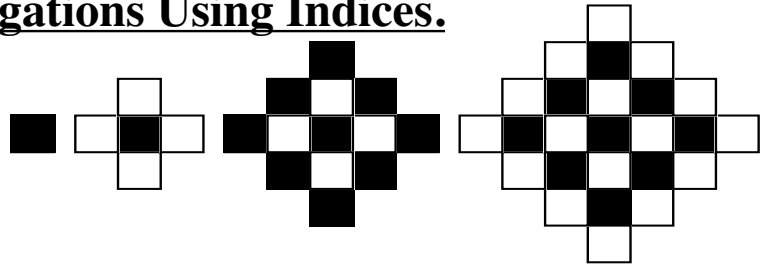
## Heading Cards

Prime Numbers	Square Numbers
Factors of 126	Factors of 60
Numbers less than 13	Numbers more than 12
Multiples of 3	Multiples of 5
Odd Numbers	Even Numbers



## Investigations Using Indices.

- 1). a). Copy this pattern on squared paper.  
 b). Continue the pattern by drawing the next three diagrams.  
 c). Investigate the number of shaded and unshaded squares in each diagram.



- 2). A chessboard is made up of 8 squares by 8 squares.  
 a). How many small squares are on this board ?  
 b). How many squares of size 2 x 2 are on this board ?  
 c). How many squares of **any** size are on this board ?  
 d). How many squares of any size are on a board of dimensions  
 i). 4 x 4;    ii). 6 x 6;    iii). 10 x 10;    iv). 20 x 20 ?



- 3).   
 1                      1 + 3 = 4                      3 + 6 = 9

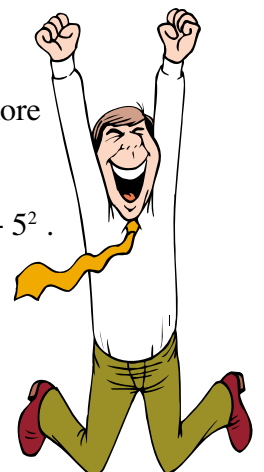
- a). Copy the pattern. Draw the next 3 in this sequence and write in the pattern of numbers.  
 b). What type of numbers are i). in bold, ii). the other numbers ?  
 c). Write an explanation of how you can make square numbers from triangular numbers.
- 4). Write out the first 30 square numbers.  
 a). Look at the last digit of these numbers. What pattern do you notice?  
 b). Which numbers don't appear as a last digit of a square number ?  
 c). Could these numbers be a square number    i). 723    ii). 1412 ?
- 5). Some numbers can be represented as the difference between two square numbers.  
 (One square number take away another square number).

$$21 = 5^2 - 2^2 \qquad 65 = 9^2 - 4^2$$

- a). There are 22 numbers up to **30** that can be written in this way. Find them.  
 b). Which whole numbers up to 30 **cannot** be represented this way ?  
 c). Which numbers up to 30 can be expressed as the difference of two squares in more than one way ?
- 6). a). Some numbers are equal to the sum of 2 square numbers.    e.g.  $34 = 3^2 + 5^2$ .  
 Which numbers up to 100 can be written as the sum of two square numbers?  
 b). Every whole number is the sum of **not more than five** square numbers.

e.g.                       $1 = 1^2$                        $2 = 1^2 + 1^2$                        $3 = 1^2 + 1^2 + 1^2$   
                                   $4 = 2^2$                        $5 = 2^2 + 1^2$

Investigate whether this is true or not.





- 7). a). Pick a number !  
 b). Square each digit and **add** the results together.  
 c). Use the new number and do the same again....  
 d). If you reach 1 you have a **happy number**.  
 e). **Sad numbers** are those that do not go to 1.  
 f). Put all the numbers up to 50 into your chains!  
 Which are happy, which are sad?

**Say 23.**

$$2^2 + 3^2 = 4 + 9 = 13$$

$$13 \quad 1^2 + 3^2 = 1 + 9 = 10$$

$$10 \quad 1^2 + 0^2 = 1 + 0 = 1$$

The 23 chain is **23 → 13 → 10 → 1**.



- 8). a). Pick any 2 digit number !  
 b). Square each digit and **subtract** the smaller from the larger.  
 c). Use the new number and do the same again....  
 d). If the answer goes to 0 it is a **sneaky number**.  
 e). **Loopy numbers** are those that do not go to 0.  
 f). Find for all the numbers up to 50 which are **sneaky** and which are **loopy**.

**Say 95**

$$9^2 - 5^2 = 81 - 25 = 56$$

$$56 \quad 6^2 - 5^2 = 36 - 25 = 11$$

$$11 \quad 1^2 - 1^2 = 0$$

The 95 chain is **95 → 56 → 11 → 0**

- 9). a). Pick a two digit number !  
 b). **Cube** each digit and **add** the results together.  
 c). Use the new number and do the same again....  
 d). Keep repeating this process. What happens ?  
 e). Try it with numbers that are one **less** than the three times table. What happens ?  
 f). Try it with numbers that are one **more** than the three times table. What happens ?

**Say 42.**

$$4^3 + 2^3 = 64 + 8 = 72$$

$$72 \quad 7^3 + 2^3 = 343 + 8 = 351$$

$$351 \quad 3^3 + 5^3 + 1^3 = 27 + 125 + 1 = 153$$

The 42 chain so far is **42 → 72 → 351 → 153**.

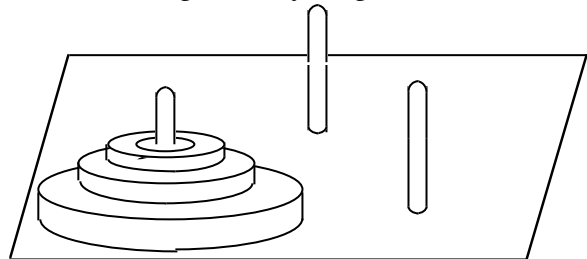
- 10). Draw Pascal's triangle and add each row. What connection with powers does it have?

- 11). You are given distance targets as sponsorship for a marathon.  
 If you complete one mile you earn 1p, if you complete two miles 2p,  
 if you complete three miles 4p and if you complete four miles 8p.  
 This pattern is continued.



- a). How much will you earn if you complete 5 miles ?  
 b). How much will you earn if you complete 10 miles ?  
 c). How much will you earn if you complete 15 miles ?  
 d). How much will you earn if you complete 20 miles ?  
 e). A marathon is 26 miles long (to the nearest mile). How much would you earn for completing the marathon ?  
 f). Can you find a formula that would work out earnings for any length of race ?

- 12). The Tower of Bramah. The idea is to move the tower, as it is, from one needle to another needle.  
 You can only move one disc at a time and there must be no smaller discs underneath the disc moved.



- a). How many moves will it take to transfer the three discs to recreate the tower ?  
 b). How many moves will it take to transfer four discs ?  
 c). How many moves will it take to transfer five discs ?  
 d). Can you find a pattern between the number of discs and the number of moves ?



# Prime Pirate Maze.

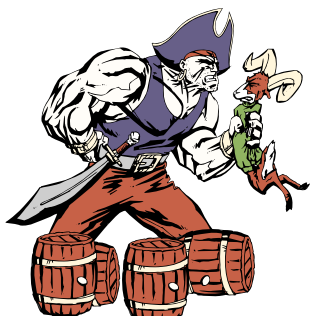


The Pirates are on the look out for treasure.  
 They can only follow a **trail of prime numbers**.  
 They can only move horizontally or vertically in the maze, **not** diagonally.  
 Only one pirate that enters the maze will find the treasure.

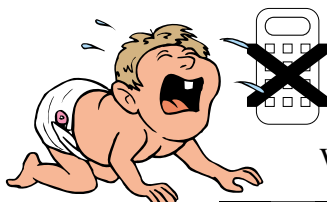
**Beware**, there are plenty of wrong trails !!!  
 Find the lucky pirate and the route he takes.



11	13	43	8	24	3	6	5	79	67	61	59	41	43	19	5	7	2	37	59	71	83	97	9	21
7	49	31	23	19	5	42	19	85	30	12	56	57	85	17	9	33	69	59	14	38	57	89	11	13
3	8	28	7	10	7	17	37	41	2	11	13	43	47	59	1	58	39	13	1	60	75	69	14	7
2	29	17	11	22	81	16	84	9	54	39	97	24	32	11	13	5	7	2	19	83	97	89	57	5
52	37	10	64	15	61	31	7	5	3	17	19	15	7	63	65	49	92	15	41	21	81	29	8	3
1	41	43	47	53	59	63	1	42	22	69	63	34	2	12	50	62	18	42	29	11	26	13	1	19
36	9	66	12	38	21	18	49	68	33	68	20	3	79	47	31	29	11	71	10	97	14	31	53	29
37	89	97	59	41	31	39	67	41	23	19	12	2	10	88	6	4	86	79	84	83	59	37	8	1
60	7	95	66	16	37	20	59	10	76	13	11	41	25	64	2	3	55	83	16	68	21	80	32	11
54	71	81	21	63	23	42	61	55	93	17	16	44	20	78	7	20	81	89	3	13	19	37	4	13
30	67	59	47	2	19	70	97	95	3	5	4	97	7	11	13	93	16	53	82	24	14	57	72	2
6	96	54	49	82	11	6	7	6	2	12	42	31	6	93	84	19	60	41	4	25	7	11	7	5
17	89	23	19	21	7	33	11	57	68	76				74	41	2	57	23	81	90	17	20	93	53
8	81	64	5	3	2	20	13	4	11	31				31	2	55	12	19	10	47	19	84	49	37
19	15	1	37	39	85	74	11	57	7	80				69	3	7	6	5	92	21	13	8	14	59
5	72	49	41	18	49	22	41	98	2	49	98	31	73	10	94	11	25	2	9	49	29	31	37	29
7	84	21	7	46	20	63	59	18	41	43	81	10	67	72	40	29	4	19	20	45	49	32	61	54
59	70	63	83	17	2	29	31	3	49	47	4	50	19	54	43	13	27	23	29	31	15	45	67	1
41	23	7	3	9	25	10	27	17	48	53	88	27	2	65	61	69	22	57	16	59	39	66	59	28
53	10	49	21	31	37	2	39	6	75	59	22	49	13	39	4	76	14	49	18	53	69	14	43	16
29	63	37	29	23	9	3	4	7	97	83	16	78	29	31	11	83	73	71	67	61	8	42	47	70
8	30	18	13	1	15	19	35	14	6	24	4	49	8	14	33	6	18	27	94	15	12	49	67	9
19	17	23	29	12	90	23	29	7	3	2	7	79	23	15	17	19	43	1	3	5	7	89	83	11
59	1	14	57	21	15	37	50	8	32	5	27	16	31	57	13	12	41	86	2	24	35	9	12	2
41	3	5	17	19	23	41	19	97	11	13	73	19	71	9	2	5	37	31	29	17	41	23	7	3



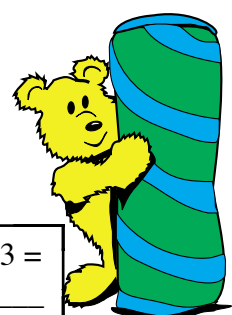
If you get time, colour all the prime numbers in on the maze.  
 This will show you all the possible pirate trails.



# A Prime Maze.

Baba has lost his teddy. He has to get through the maze to find it. He can only travel along **prime numbers**.

Work out each sum. Now find the route he must take to find his teddy.

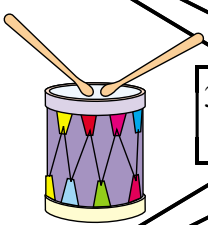


IN     $20 - 7 =$      $6 \times 10 =$      $90 - 11 =$      $99 \div 3 =$      $39 \div 3 =$

$2 \times 17 =$      $103 - 44 =$      $5 \times 9 =$      $58 \div 2 =$      $27 + 34 =$      $3 \times 31 =$

$19 + 18 =$      $55 \div 5 =$      $50 - 13 =$      $110 \div 2 =$      $75 - 62 =$

$49 + 18 =$      $17 \times 2 =$      $72 \div 3 =$      $38 + 58 =$      $45 - 18 =$      $100 \div 20 =$



$36 + 43 =$      $6 \times 9 =$      $85 - 24 =$      $18 + 29 =$      $92 \div 4 =$

$95 \div 5 =$      $23 \times 3 =$      $76 \div 38 =$      $98 - 74 =$      $57 \div 57 =$      $90 \div 6 =$

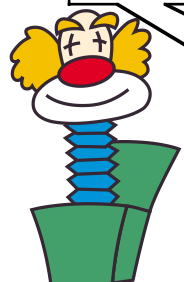
$5 \times 10 =$      $64 - 35 =$      $81 - 62 =$      $64 - 47 =$      $17 + 24 =$



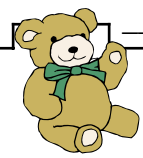
$105 \div 5 =$      $91 \div 13 =$      $150 \div 6 =$      $24 \times 4 =$      $15 \times 5 =$      $105 - 68 =$

$4 \times 22 =$      $106 - 65 =$      $19 + 64 =$      $108 \div 12 =$      $63 \div 9 =$

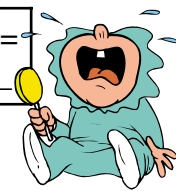
$4 \times 16 =$      $92 \div 4 =$      $6 \times 13 =$      $77 \div 7 =$      $165 \div 5 =$      $93 - 69 =$



$9 \times 9 =$      $79 - 32 =$      $9 \times 6 =$      $25 + 48 =$      $39 + 58 =$



OUT

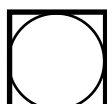




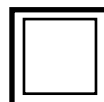
# Prime and Square Numbers

Roll the dice. Move forward that many places. If you land on a **prime** number move forwards to the next prime number. If you land on a **square** number move back to the previous square number.

Start	1	2	3	4	5	6	7	8	9	10	11
											12
24	23	22	21	20	19	18	17	16	15	14	13
25											
26	27	28	29	30	31	32	33	34	35	36	37
											38
50	49	48	47	46	45	44	43	42	41	40	39
51											
52	53	54	55	56	57	58	59	60	61	62	63
											64
76	75	74	73	72	71	70	69	68	67	66	65
77											
78	79	80	81	82	83	84	85	86	87	88	89
											90
WIN	100	99	98	97	96	95	94	93	92	91	



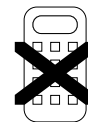
Move **forward** to the next **prime** number



Move **back** to the last **square** number



## Multiplying by Powers of 10.



A). Multiply the following by **10**.

- |             |             |             |              |              |
|-------------|-------------|-------------|--------------|--------------|
| 1). 5       | 2). 8       | 3). 13      | 4). 21       | 5). 18       |
| 6). 17      | 7). 38      | 8). 41      | 9). 37       | 10). 89      |
| 11). 124    | 12). 274    | 13). 579    | 14). 935     | 15). 5834    |
| 16). 3403   | 17). 2056   | 18). 9153   | 19). 6728    | 20). 6241    |
| 21). 4.6    | 22). 9.3    | 23). 16.6   | 24). 28.2    | 25). 30.6    |
| 26). 0.8    | 27). 46.9   | 28). 234.9  | 29). 0.6     | 30). 49.3    |
| 31). 2.35   | 32). 7.26   | 33). 0.42   | 34). 5.06    | 35). 9.88    |
| 36). 14.56  | 37). 45.08  | 38). 50.21  | 39). 0.89    | 40). 345.68  |
| 41). 5.682  | 42). 0.083  | 43). 7.572  | 44). 9.803   | 45). 3.719   |
| 46). 16.682 | 47). 25.904 | 48). 98.455 | 49). 234.987 | 50). 382.892 |

B). Multiply the following by **100**.

- |             |             |             |            |              |
|-------------|-------------|-------------|------------|--------------|
| 1). 7       | 2). 2       | 3). 17      | 4). 29     | 5). 48       |
| 6). 67      | 7). 48      | 8). 47      | 9). 27     | 10). 99      |
| 11). 164    | 12). 374    | 13). 679    | 14). 335   | 15). 7834    |
| 16). 3803   | 17). 6056   | 18). 8153   | 19). 2728  | 20). 5221    |
| 21). 4.54   | 22). 9.26   | 23). 16.73  | 24). 28.18 | 25). 30.08   |
| 26). 0.16   | 27). 46.82  | 28). 234.47 | 29). 0.82  | 30). 49.62   |
| 31). 1.793  | 32). 3.279  | 33). 0.479  | 34). 4.092 | 35). 1.891   |
| 36). 14.312 | 37). 45.037 | 38). 50.821 | 39). 0.512 | 40). 345.069 |
| 41). 4.6    | 42). 3.8    | 43). 0.5    | 44). 7.8   | 45). 2.7     |
| 46). 36.6   | 47). 15.9   | 48). 28.4   | 49). 734.9 | 50). 882.8   |

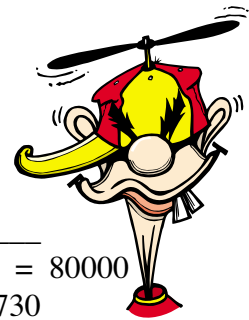
C). Multiply the following by **1000**.

- |            |             |              |             |             |
|------------|-------------|--------------|-------------|-------------|
| 1). 5      | 2). 1       | 3). 12       | 4). 24      | 5). 78      |
| 6). 27     | 7). 98      | 8). 46       | 9). 97      | 10). 89     |
| 11). 124   | 12). 574    | 13). 179     | 14). 235    | 15). 6824   |
| 16). 7803  | 17). 2057   | 18). 7153    | 19). 3728   | 20). 9201   |
| 21). 4.592 | 22). 9.682  | 23). 26.054  | 24). 48.102 | 25). 10.731 |
| 26). 0.931 | 27). 26.804 | 28). 434.933 | 29). 0.951  | 30). 39.782 |
| 31). 1.49  | 32). 3.27   | 33). 0.47    | 34). 7.08   | 35). 1.89   |
| 36). 84.31 | 37). 25.03  | 38). 30.82   | 39). 0.51   | 40). 545.07 |
| 41). 3.7   | 42). 5.9    | 43). 0.2     | 44). 3.8    | 45). 1.7    |
| 46). 26.3  | 47). 65.1   | 48). 18.9    | 49). 234.5  | 50). 782.9  |



D). Copy the questions and work out the answer.

- |                         |                         |                         |                         |                           |
|-------------------------|-------------------------|-------------------------|-------------------------|---------------------------|
| 1). $5 \times 100$      | 2). $7 \times 10000$    | 3). $12 \times 1000$    | 4). $43 \times 10000$   | 5). $68 \times 100$       |
| 6). $76 \times 1000$    | 7). $56 \times 100$     | 8). $86 \times 10$      | 9). $51 \times 1000$    | 10). $25 \times 10000$    |
| 11). $262 \times 100$   | 12). $541 \times 10$    | 13). $948 \times 1000$  | 14). $342 \times 10$    | 15). $702 \times 1000$    |
| 16). $6503 \times 100$  | 17). $7023 \times 10$   | 18). $9003 \times 100$  | 19). $3401 \times 10$   | 20). $3057 \times 1000$   |
| 21). $4.046 \times 10$  | 22). $3.642 \times 100$ | 23). $6.054 \times 10$  | 24). $1.102 \times 100$ | 25). $0.7391 \times 1000$ |
| 26). $0.931 \times 100$ | 27). $26.804 \times 10$ | 28). $4.133 \times 100$ | 29). $0.951 \times 100$ | 30). $49.782 \times 1000$ |
| 31). $0.49 \times 10$   | 32). $3.27 \times 100$  | 33). $0.27 \times 100$  | 34). $7.01 \times 10$   | 35). $6.959 \times 1000$  |
| 36). $4.31 \times 100$  | 37). $25.03 \times 10$  | 38). $30.82 \times 10$  | 39). $0.51 \times 100$  | 40). $345.08 \times 1000$ |
| 41). $3.7 \times 1000$  | 42). $5.9 \times 100$   | 43). $0.2 \times 100$   | 44). $3.8 \times 1000$  | 45). $1.7 \times 10000$   |
| 46). $16.3 \times 100$  | 47). $55.1 \times 10$   | 48). $38.9 \times 100$  | 49). $834.5 \times 10$  | 50). $582.9 \times 10000$ |



E). Copy the questions and fill in the missing values.

- |  |  |  |
|--|--|--|
| 1). $6 \times \underline{\quad} = 60$        | 2). $\underline{\quad} \times 100 = 500$     | 3). $9 \times 1000 = \underline{\quad}$        |
| 4). $\underline{\quad} \times 10 = 70$       | 5). $3 \times \underline{\quad} = 3000$      | 6). $\underline{\quad} \times 10000 = 80000$   |
| 7). $16 \times 1000 = \underline{\quad}$     | 8). $\underline{\quad} \times 100 = 5000$    | 9). $73 \times \underline{\quad} = 730$        |
| 10). $\underline{\quad} \times 100 = 5600$   | 11). $68 \times 1000 = \underline{\quad}$    | 12). $\underline{\quad} \times 1000 = 93000$   |
| 13). $4.7 \times 10000 = \underline{\quad}$  | 14). $\underline{\quad} \times 10 = 67$      | 15). $9.7 \times \underline{\quad} = 97000$    |
| 16). $0.8 \times \underline{\quad} = 800$    | 17). $1.7 \times 1000 = \underline{\quad}$   | 18). $6.3 \times \underline{\quad} = 63$       |
| 19). $31.3 \times \underline{\quad} = 3130$  | 20). $\underline{\quad} \times 100 = 1230$   | 21). $\underline{\quad} \times 1000 = 89300$   |
| 22). $47.5 \times \underline{\quad} = 475$   | 23). $0.5 \times \underline{\quad} = 5000$   | 24). $2.1 \times 100 = \underline{\quad}$      |
| 25). $3.42 \times 1000 = \underline{\quad}$  | 26). $5.62 \times \underline{\quad} = 562$   | 27). $9.03 \times \underline{\quad} = 9030$    |
| 28). $\underline{\quad} \times 100 = 341$    | 29). $\underline{\quad} \times 10 = 3.4$     | 30). $6.01 \times 1000 = \underline{\quad}$    |
| 31). $0.67 \times \underline{\quad} = 6700$  | 32). $\underline{\quad} \times 10 = 6$       | 33). $\underline{\quad} \times 1000 = 70$      |
| 34). $0.03 \times 10000 = \underline{\quad}$ | 35). $5.08 \times 1000 = \underline{\quad}$  | 36). $\underline{\quad} \times 100 = 8$        |
| 37). $\underline{\quad} \times 10 = 54.36$   | 38). $7.009 \times 100 = \underline{\quad}$  | 39). $\underline{\quad} \times 10000 = 134.56$ |
| 40). $0.004 \times \underline{\quad} = 0.4$  | 41). $6.781 \times \underline{\quad} = 6781$ | 42). $\underline{\quad} \times 10 = 0.37$      |
| 43). $\underline{\quad} \times 100 = 7.4$    | 44). $0.001 \times \underline{\quad} = 0.01$ | 45). $3.008 \times 1000 = \underline{\quad}$   |

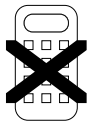
F). Copy the questions and work out the answer.

- |                          |                           |                          |                          |                           |
|--------------------------|---------------------------|--------------------------|--------------------------|---------------------------|
| 1). $4 \times 10^2$      | 2). $3 \times 10^1$       | 3). $11 \times 10^3$     | 4). $23 \times 10^4$     | 5). $18 \times 10^3$      |
| 6). $86 \times 10^4$     | 7). $26 \times 10^2$      | 8). $16 \times 10^1$     | 9). $91 \times 10^3$     | 10). $35 \times 10^1$     |
| 11). $242 \times 10^1$   | 12). $501 \times 10^3$    | 13). $148 \times 10^2$   | 14). $442 \times 10^1$   | 15). $202 \times 10^3$    |
| 16). $1503 \times 10^1$  | 17). $8023 \times 10^3$   | 18). $1003 \times 10^4$  | 19). $6405 \times 10^2$  | 20). $1059 \times 10^1$   |
| 21). $3.086 \times 10^2$ | 22). $1.642 \times 10^3$  | 23). $2.074 \times 10^1$ | 24). $1.002 \times 10^4$ | 25). $0.031 \times 10^1$  |
| 26). $0.301 \times 10^3$ | 27). $16.104 \times 10^2$ | 28). $3.138 \times 10^3$ | 29). $0.251 \times 10^1$ | 30). $89.182 \times 10^2$ |
| 31). $0.19 \times 10^2$  | 32). $8.67 \times 10^1$   | 33). $5.27 \times 10^3$  | 34). $0.05 \times 10^1$  | 35). $4.89 \times 10^2$   |
| 36). $8.32 \times 10^4$  | 37). $75.83 \times 10^1$  | 38). $40.74 \times 10^3$ | 39). $0.51 \times 10^3$  | 40). $375.08 \times 10^2$ |
| 41). $8.7 \times 10^1$   | 42). $2.9 \times 10^3$    | 43). $5.2 \times 10^4$   | 44). $0.8 \times 10^4$   | 45). $3.7 \times 10^2$    |
| 46). $73.3 \times 10^2$  | 47). $47.1 \times 10^4$   | 48). $74.9 \times 10^1$  | 49). $835.5 \times 10^1$ | 50). $372.9 \times 10^4$  |

G). Copy the questions and fill in the missing values.

- |  |  |   |
|--|--|---|
| 1). $\underline{\quad} \times 10^2 = 800$    | 2). $\underline{\quad} \times 10^1 = 700$    | 3). $3 \times 10^2 = \underline{\quad}$       |
| 4). $\underline{\quad} \times 10^4 = 20000$  | 5). $8 \times \underline{\quad} = 8000$      | 6). $\underline{\quad} \times 10^3 = 9000$    |
| 7). $36 \times 10^3 = \underline{\quad}$     | 8). $\underline{\quad} \times 10^2 = 7000$   | 9). $23 \times \underline{\quad} = 230$       |
| 10). $\underline{\quad} \times 10^1 = 5600$  | 11). $68 \times 10^1 = \underline{\quad}$    | 12). $\underline{\quad} \times 10^3 = 93000$  |
| 13). $4.7 \times 10^2 = \underline{\quad}$   | 14). $\underline{\quad} \times 10^1 = 47$    | 15). $1.7 \times \underline{\quad} = 170$     |
| 16). $0.4 \times \underline{\quad} = 4000$   | 17). $1.7 \times 10^2 = \underline{\quad}$   | 18). $8.3 \times \underline{\quad} = 83$      |
| 19). $21.3 \times \underline{\quad} = 2130$  | 20). $\underline{\quad} \times 10^1 = 13$    | 21). $\underline{\quad} \times 10^3 = 19300$  |
| 22). $42.5 \times \underline{\quad} = 425$   | 23). $0.1 \times \underline{\quad} = 10$     | 24). $7.1 \times 10^2 = \underline{\quad}$    |
| 25). $3.02 \times 10^3 = \underline{\quad}$  | 26). $2.62 \times \underline{\quad} = 262$   | 27). $3.03 \times \underline{\quad} = 3030$   |
| 28). $\underline{\quad} \times 10^2 = 541$   | 29). $\underline{\quad} \times 10^2 = 8$     | 30). $9.02 \times 10^2 = \underline{\quad}$   |
| 31). $0.34 \times \underline{\quad} = 340$   | 32). $\underline{\quad} \times 10^1 = 2$     | 33). $\underline{\quad} \times 10^4 = 700$    |
| 34). $0.07 \times 10^4 = \underline{\quad}$  | 35). $2.03 \times 10^3 = \underline{\quad}$  | 36). $\underline{\quad} \times 10^1 = 0.8$    |
| 37). $\underline{\quad} \times 10^1 = 14.36$ | 38). $7.009 \times 10^3 = \underline{\quad}$ | 39). $\underline{\quad} \times 10^1 = 134.56$ |
| 40). $0.005 \times \underline{\quad} = 50$   | 41). $1.781 \times \underline{\quad} = 1781$ | 42). $\underline{\quad} \times 10^2 = 0.3$    |
| 43). $\underline{\quad} \times 10^2 = 7.4$   | 44). $0.004 \times \underline{\quad} = 0.04$ | 45). $8.002 \times 10^3 = \underline{\quad}$  |





## Dividing by Powers of 10.



A). Divide the following by **10**.

- |              |              |              |              |              |
|--------------|--------------|--------------|--------------|--------------|
| 1). 70       | 2). 40       | 3). 90       | 4). 120      | 5). 160      |
| 6). 320      | 7). 390      | 8). 420      | 9). 370      | 10). 890     |
| 11). 1240    | 12). 2340    | 13). 5580    | 14). 9290    | 15). 5700    |
| 16). 34430   | 17). 20050   | 18). 34830   | 19). 67800   | 20). 62000   |
| 21). 49      | 22). 92      | 23). 12      | 24). 28      | 25). 39      |
| 26). 73      | 27). 98      | 28). 7       | 29). 63      | 30). 3       |
| 31). 13.7    | 32). 45.9    | 33). 98.2    | 34). 40.1    | 35). 75.6    |
| 36). 135.3   | 37). 232.6   | 38). 634.1   | 39). 6.2     | 40). 3.74    |
| 41). 0.59    | 42). 10.03   | 43). 57.72   | 44). 89.03   | 45). 56.79   |
| 46). 316.682 | 47). 525.904 | 48). 198.455 | 49). 234.987 | 50). 382.892 |

B). Divide the following by **100**.

- |            |            |            |            |            |
|------------|------------|------------|------------|------------|
| 1). 800    | 2). 200    | 3). 1700   | 4). 2900   | 5). 4800   |
| 6). 6700   | 7). 4800   | 8). 4700   | 9). 2700   | 10). 9900  |
| 11). 1640  | 12). 3740  | 13). 6790  | 14). 3350  | 15). 7830  |
| 16). 3880  | 17). 6050  | 18). 8150  | 19). 2720  | 20). 5220  |
| 21). 454   | 22). 926   | 23). 1673  | 24). 2818  | 25). 3008  |
| 26). 16    | 27). 4682  | 28). 2347  | 29). 82    | 30). 4     |
| 31). 31.7  | 32). 23.2  | 33). 56.7  | 34). 14.2  | 35). 81.1  |
| 36). 4.12  | 37). 0.07  | 38). 8.81  | 39). 324.5 | 40). 945.9 |
| 41). 4.6   | 42). 453.8 | 43). 0.4   | 44). 7.8   | 45). 9.7   |
| 46). 436.6 | 47). 1.879 | 48). 428.4 | 49). 73.39 | 50). 0.002 |

C). Divide the following by **1000**.

- |              |             |             |              |               |
|--------------|-------------|-------------|--------------|---------------|
| 1). 5000     | 2). 1000    | 3). 42000   | 4). 74000    | 5). 38000     |
| 6). 17000    | 7). 54000   | 8). 7000    | 9). 29000    | 10). 89000    |
| 11). 1600    | 12). 7200   | 13). 27900  | 14). 22900   | 15). 60700    |
| 16). 200     | 17). 8500   | 18). 16700  | 19). 3700    | 20). 600      |
| 21). 4592    | 22). 9682   | 23). 2754   | 24). 4102    | 25). 1731     |
| 26). 931     | 27). 804    | 28). 933    | 29). 951     | 30). 782      |
| 31). 568.7   | 32). 6794.2 | 33). 9803.6 | 34). 957.2   | 35). 2003.5   |
| 36). 84.1    | 37). 25.3   | 38). 30.2   | 39). 9.5     | 40). 545.7    |
| 41). 3.74    | 42). 5.95   | 43). 57.24  | 44). 3891.86 | 45). 1.79     |
| 46). 2646.31 | 47). 605.12 | 48). 18.08  | 49). 4.57    | 50). 71282.93 |



D). Copy the questions and work out the answer.

- |                      |                      |                       |                      |                         |
|----------------------|----------------------|-----------------------|----------------------|-------------------------|
| 1). $500 \div 100$   | 2). $70 \div 10$     | 3). $9000 \div 100$   | 4). $4300 \div 10$   | 5). $6000 \div 1000$    |
| 6). $76 \div 10$     | 7). $560 \div 100$   | 8). $860 \div 100$    | 9). $51 \div 10$     | 10). $5700 \div 1000$   |
| 11). $8 \div 10$     | 12). $46 \div 100$   | 13). $580 \div 1000$  | 14). $34 \div 100$   | 15). $720 \div 1000$    |
| 16). $653 \div 100$  | 17). $7023 \div 10$  | 18). $903 \div 100$   | 19). $3401 \div 100$ | 20). $57 \div 1000$     |
| 21). $4.6 \div 10$   | 22). $3.2 \div 100$  | 23). $6.4 \div 1000$  | 24). $1.2 \div 100$  | 25). $0.7 \div 10$      |
| 26). $0.91 \div 10$  | 27). $6.88 \div 100$ | 28). $4.03 \div 1000$ | 29). $0.71 \div 10$  | 30). $49.78 \div 1000$  |
| 31). $8.9 \div 10$   | 32). $327 \div 100$  | 33). $27 \div 1000$   | 34). $7.01 \div 100$ | 35). $6.99 \div 10$     |
| 36). $31 \div 100$   | 37). $2503 \div 10$  | 38). $30.82 \div 10$  | 39). $0.51 \div 100$ | 40). $345.08 \div 1000$ |
| 41). $9.7 \div 1000$ | 42). $59 \div 1000$  | 43). $0.2 \div 100$   | 44). $3.8 \div 10$   | 45). $1.7 \div 1000$    |
| 46). $26.3 \div 100$ | 47). $55.1 \div 10$  | 48). $38.9 \div 100$  | 49). $834.5 \div 10$ | 50). $2.09 \div 1000$   |



E). Copy the questions and fill in the missing values.

- |   |  |  |
|---|--|--|
| 1). $60 \div \underline{\quad} = 6$       | 2). $\underline{\quad} \div 100 = 5$       | 3). $9000 \div 1000 = \underline{\quad}$   |
| 4). $\underline{\quad} \div 10 = 70$      | 5). $3000 \div \underline{\quad} = 30$     | 6). $\underline{\quad} \div 100 = 80$      |
| 7). $1600 \div 1000 = \underline{\quad}$  | 8). $\underline{\quad} \div 100 = 5.6$     | 9). $7300 \div \underline{\quad} = 730$    |
| 10). $\underline{\quad} \div 100 = 720$   | 11). $680 \div 1000 = \underline{\quad}$   | 12). $\underline{\quad} \div 1000 = 9.3$   |
| 13). $47 \div 100 = \underline{\quad}$    | 14). $\underline{\quad} \div 10 = 0.6$     | 15). $970 \div \underline{\quad} = 9.7$    |
| 16). $800 \div \underline{\quad} = 0.8$   | 17). $170 \div 1000 = \underline{\quad}$   | 18). $6.3 \div \underline{\quad} = 0.63$   |
| 19). $313 \div \underline{\quad} = 3.13$  | 20). $\underline{\quad} \div 100 = 12.3$   | 21). $\underline{\quad} \div 1000 = 89.3$  |
| 22). $475 \div \underline{\quad} = 47.5$  | 23). $50 \div \underline{\quad} = 0.5$     | 24). $21 \div 100 = \underline{\quad}$     |
| 25). $34.2 \div 1000 = \underline{\quad}$ | 26). $562 \div \underline{\quad} = 56.2$   | 27). $903 \div \underline{\quad} = 9.03$   |
| 28). $\underline{\quad} \div 100 = 34.1$  | 29). $\underline{\quad} \div 10 = 3.4$     | 30). $601 \div 100 = \underline{\quad}$    |
| 31). $67 \div \underline{\quad} = 0.67$   | 32). $\underline{\quad} \div 10 = 6$       | 33). $\underline{\quad} \div 1000 = 70$    |
| 34). $0.3 \div 10 = \underline{\quad}$    | 35). $58 \div 1000 = \underline{\quad}$    | 36). $\underline{\quad} \div 100 = 0.07$   |
| 37). $\underline{\quad} \div 10 = 54.36$  | 38). $7009 \div 100 = \underline{\quad}$   | 39). $\underline{\quad} \div 10 = 134.56$  |
| 40). $0.4 \div \underline{\quad} = 0.004$ | 41). $6781 \div \underline{\quad} = 6.781$ | 42). $\underline{\quad} \div 10 = 0.37$    |
| 43). $\underline{\quad} \div 100 = 7.4$   | 44). $0.01 \div \underline{\quad} = 0.001$ | 45). $30.08 \div 1000 = \underline{\quad}$ |

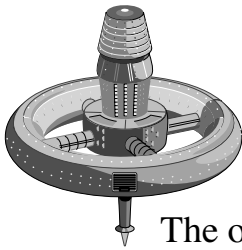
F). Copy the questions and work out the answer.

- |                        |                        |                        |                        |                         |
|------------------------|------------------------|------------------------|------------------------|-------------------------|
| 1). $478 \div 10^2$    | 2). $96 \div 10^1$     | 3). $1200 \div 10^3$   | 4). $2300 \div 10^4$   | 5). $1800 \div 10^3$    |
| 6). $8670 \div 10^4$   | 7). $78 \div 10^2$     | 8). $76 \div 10^1$     | 9). $591 \div 10^3$    | 10). $385 \div 10^1$    |
| 11). $242 \div 10^1$   | 12). $501 \div 10^3$   | 13). $148 \div 10^2$   | 14). $442 \div 10^1$   | 15). $202 \div 10^3$    |
| 16). $1.3 \div 10^1$   | 17). $803 \div 10^3$   | 18). $1003 \div 10^4$  | 19). $605 \div 10^2$   | 20). $1059 \div 10^1$   |
| 21). $38.6 \div 10^2$  | 22). $164.2 \div 10^3$ | 23). $27.4 \div 10^1$  | 24). $100.2 \div 10^4$ | 25). $0.031 \div 10^1$  |
| 26). $0.301 \div 10^2$ | 27). $16.14 \div 10^2$ | 28). $3.138 \div 10^3$ | 29). $0.251 \div 10^1$ | 30). $89.182 \div 10^2$ |
| 31). $7.19 \div 10^2$  | 32). $8.67 \div 10^1$  | 33). $5.27 \div 10^3$  | 34). $0.05 \div 10^1$  | 35). $4.89 \div 10^2$   |
| 36). $882 \div 10^4$   | 37). $75.83 \div 10^1$ | 38). $4074 \div 10^3$  | 39). $51 \div 10^3$    | 40). $37508 \div 10^2$  |
| 41). $8.7 \div 10^1$   | 42). $2.9 \div 10^3$   | 43). $5.2 \div 10^4$   | 44). $0.8 \div 10^4$   | 45). $3.7 \div 10^2$    |
| 46). $73.3 \div 10^2$  | 47). $4710 \div 10^4$  | 48). $749 \div 10^1$   | 49). $835 \div 10^1$   | 50). $302.9 \div 10^4$  |

G). Copy the questions and fill in the missing values.

- |   |   |   |
|---|---|---|
| 1). $\underline{\quad} \div 10^2 = 4$       | 2). $\underline{\quad} \div 10^1 = 50$      | 3). $300 \div 10^2 = \underline{\quad}$     |
| 4). $\underline{\quad} \div 10^4 = 3$       | 5). $700 \div \underline{\quad} = 7$        | 6). $\underline{\quad} \div 10^3 = 12$      |
| 7). $360 \div 10^3 = \underline{\quad}$     | 8). $\underline{\quad} \div 10^2 = 7.2$     | 9). $290 \div \underline{\quad} = 2.9$      |
| 10). $\underline{\quad} \div 10^1 = 5.7$    | 11). $68 \div 10^1 = \underline{\quad}$     | 12). $\underline{\quad} \div 10^3 = 9.8$    |
| 13). $47 \div 10^2 = \underline{\quad}$     | 14). $\underline{\quad} \div 10^1 = 47$     | 15). $17 \div \underline{\quad} = 0.017$    |
| 16). $4000 \div \underline{\quad} = 0.4$    | 17). $19 \div 10^2 = \underline{\quad}$     | 18). $83 \div \underline{\quad} = 8.3$      |
| 19). $2180 \div \underline{\quad} = 2.18$   | 20). $\underline{\quad} \div 10^1 = 13$     | 21). $\underline{\quad} \div 10^3 = 19$     |
| 22). $425 \div \underline{\quad} = 42.5$    | 23). $100 \div \underline{\quad} = 0.1$     | 24). $0.6 \div 10^1 = \underline{\quad}$    |
| 25). $3.02 \div 10^3 = \underline{\quad}$   | 26). $2.62 \div \underline{\quad} = 0.262$  | 27). $303 \div \underline{\quad} = 0.0303$  |
| 28). $\underline{\quad} \div 10^2 = 5.41$   | 29). $\underline{\quad} \div 10^2 = 0.006$  | 30). $9.02 \div 10^2 = \underline{\quad}$   |
| 31). $4 \div \underline{\quad} = 0.004$     | 32). $\underline{\quad} \div 10^1 = 2$      | 33). $\underline{\quad} \div 10^4 = 3$      |
| 34). $0.7 \div 10^2 = \underline{\quad}$    | 35). $203 \div 10^3 = \underline{\quad}$    | 36). $\underline{\quad} \div 10^1 = 0.008$  |
| 37). $\underline{\quad} \div 10^1 = 14.36$  | 38). $7.009 \div 10^3 = \underline{\quad}$  | 39). $\underline{\quad} \div 10^1 = 134.56$ |
| 40). $0.05 \div \underline{\quad} = 0.0005$ | 41). $1.71 \div \underline{\quad} = 0.171$  | 42). $\underline{\quad} \div 10^2 = 0.3$    |
| 43). $\underline{\quad} \div 10^2 = 7.4$    | 44). $0.4 \div \underline{\quad} = 0.00004$ | 45). $68.002 \div 10^3 = \underline{\quad}$ |





# Zap to Zero.



The aliens are coming to town.

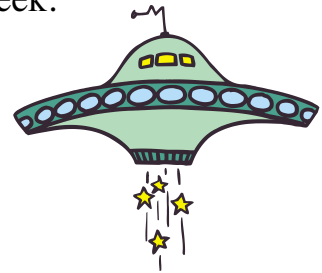
The only way to annihilate them is to **zap them to zero**.

Captain Slog keeps careful records of every alien's number he zaps.

He is very orderly about it. He always zaps the smallest digit first in the alien's number. He then works his way up to the biggest digit.

His last encounter was with the alien formerly known as 4792.316, a cheeky green chappie from the planet Geek.

Here is Captain Slog's Log.



Keys Used	Calculator Display
<b>Start</b>	4792.316
x 100	479231.6
- 1	479230.6
÷ 100	4792.306
- 2	4790.306
x 10	47903.06
- 3	47900.06
÷ 10000	4.790006
- 4	0.790006
x 1000000	790006
- 6	790000
÷ 100000	7.9
- 7	0.9
x 10	9
- 9	0

*Aliens Trashed!*

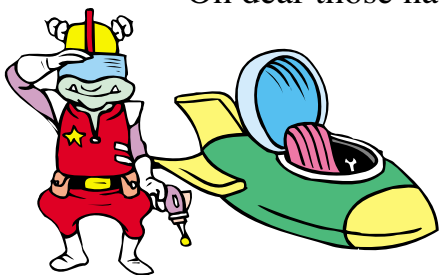
Here are the Captain's Rules of Encounter.

- 1). Enter the alien's number into your calculator.
- 2). You zap an alien by turning it into zeros.
- 3). You can only zap an alien in the units column by subtracting.
- 4). The alien's number has to be zapped from smallest to biggest digit.
- 5). You can multiply or divide by 10, 100, 1000, ....
- 6). All zapping must be recorded in Captain Slog's Log.
- 7). **Only the brave survive.**

Oh dear those naughty Geeks are attacking Earth's defences again.

Captain Slog is on holiday.

Only you can help.

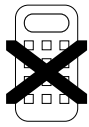


## *Be ruthless.*



Here are the names of the "alien eight".

- |             |             |              |              |
|-------------|-------------|--------------|--------------|
| 1). 374.18  | 2). 6513.4  | 3). 714.59   | 4). 1732.64  |
| 5). 739.216 | 6). 2513.96 | 7). 1578.324 | 8). 631.9427 |



# Stamps.



- 1). Jim works in a small village Post Office and it has run out of stamps. When the new stamps arrive there are only 4p and 7p stamps.
  - a). Which stamps does he need to put on a letter that needs the value
    - i). 20 p,      ii). 24p,      ii). 25p,      iv). 33p ?
  - b).
    - i). Which values **can't** he make ?
    - ii). What is the largest value he can't make ?
  - c).
    - i). Investigate other **pairs** of stamps. For these pairs look for the largest values he **can't** make?
    - ii). Try to find a general formula for the largest value a pair of stamps x and y **can't** make.
  - d). Hence, or otherwise, find the largest value the following pairs of stamps **can't** make
    - i). 5p and 8p,      ii). 11p and 12p,      iii). 22p and 25p.



- 2). Jim rings up head office for more stamps. This time they only send him 1p and 2p stamps. He looks at all the ways he can make the value 3p. He finds 3 ways.
- (Notice the order of the stamps is important. 1p, 2p is different from 2p, 1p).



- a). How many ways can he make the value of 4p ?
- b). Investigate how many ways he can make other values.
- c). This pattern has name. What is it ?

- 3). When the Post office is shut the stamps can be bought from a machine outside. The machine dispenses books with 5 stamps in it. The books have to make up **all consecutive** values without any gaps. For example, this book of 5 stamps could make up the values: 1p, 2p, 3p, 4p, 5p, 6p and 7p. 7 consecutive values in total.

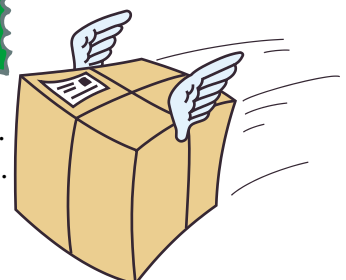


Investigate the values other books of 5 stamps can make.  
What are the values of the 5 stamps that make the **most** number of consecutive values ?

- 4). A new book of 7 stamps is introduced.

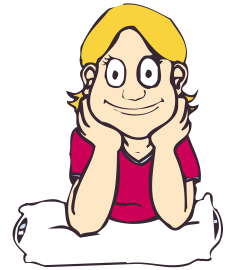


This book has stamps of value 1p, 2p, 5p, 10p, 20p, 50p and £1.  
Investigate the different values that can be made from this book.

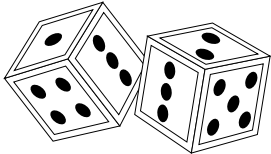
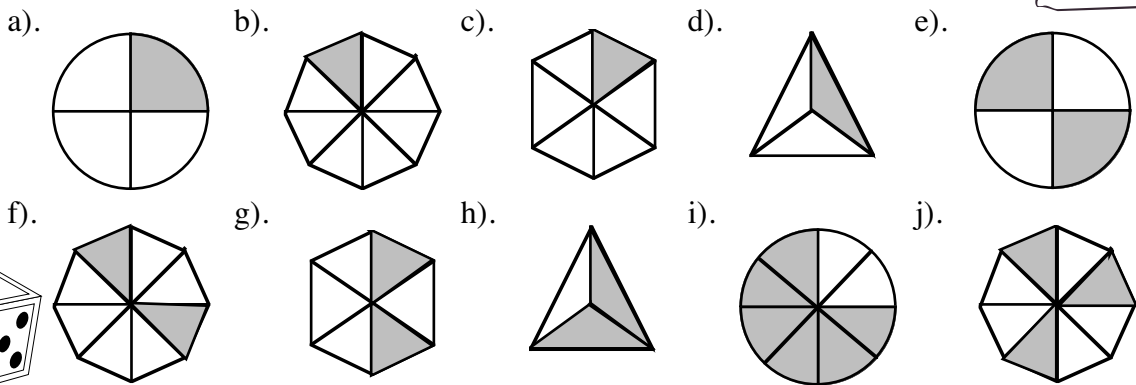




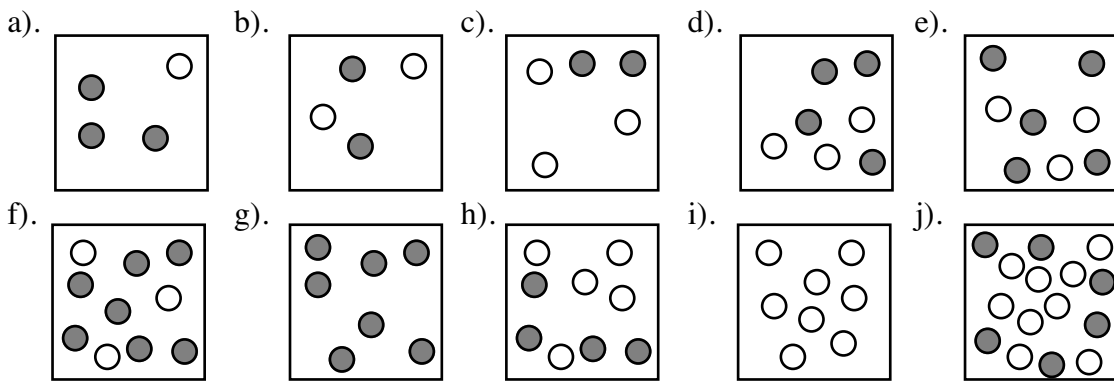
# Probability (Equally Likely Outcomes).



1). The following fair spinners are spun. What is the probability of landing on the shaded section for each spinner ?



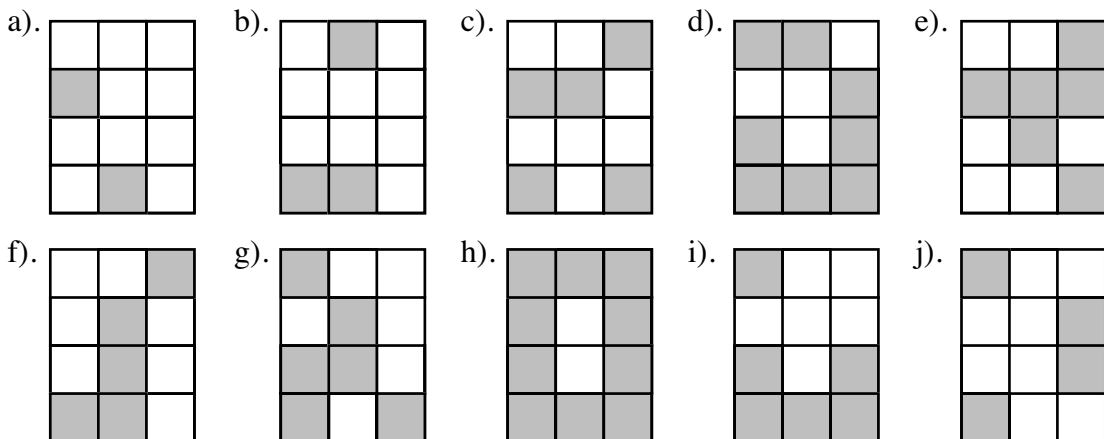
2). Counters are placed in a box. For each of the following boxes, find the probability of a shaded counter being drawn out of the box at random.



3). If a fair six-sided dice is thrown, what is the probability that the score is :-

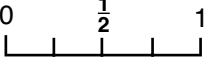
- a). a 5 (five)      b). an even number      c). an odd number  
d). a prime number      e). a square number      f). greater than 4 ?

4). In a game you throw a coin onto a board. It will always land exactly on one square. If you land on a shaded square you win. Find the probability of winning on the following boards.



- k). Which of these boards are "fair" ?  
l). Which board would you like to play on, because you would be most likely to win ?  
m). Which board would you **not** like to play on, because you would be most likely to lose?

- 5). Ten counters are placed in a box. The counters are labelled A, B, C, D, E, F, G, H, I and J. If one counter is drawn at random from the box find the probability that it is :-  
 a). a vowel                      b). a consonant                      c). a D ?

- 6).  Draw the number line in your book. The number line represents all possible probabilities. Indicate, using arrows labelled "a" to "f" the probabilities for :-

- a). throwing a HEAD on a coin;                      b). cutting a spade from a pack of cards;  
 c). May following April;                      d). the electricity being cut off today;  
 e). scoring a 1 or a 6 on a dice;                      f). scoring 23 with one dart on a dartboard.

- 7). There are 12 counters in a box. The counters are numbered 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, and 12. If one counter is drawn out at random, what is the probability that it is a counter :-  
 a). with an odd number                      b). with an even number  
 c). with a square number                      d). that is greater than or equal to 8 ?

- 8). I have a pack of playing cards, containing 52 cards. I pick a card at random. What is the probability that the card I select is :-  
 a). a king                      b). an ace                      c). a diamond  
 d). a red card                      e). a 10 (ten)                      f). the queen of Spades ?

- 9). Writing pads are available in 4 different colours. In a pack there are 6 blue, 8 red, 14 white and 18 green. What is the probability when I open a new pack I randomly pick a :-  
 a). blue pad                      b). red pad                      c). white pad  
 d). green pad                      e). yellow pad                      f). red or white pad ?

- 10). A bag contains 6 blue discs, 10 orange discs and 4 red discs. If a disc is picked at random what is the probability of getting :-  
 a). a blue disc                      b). an orange disc                      c). a blue or red disc  
 d). a blue or orange disc                      e). **not** an orange disc                      f). a blue, orange or red disc?

- 11). A small box of chocolates contains 6 hard centres, 8 soft centres and 12 chewy centres. What is the probability of picking :-  
 a). a hard centre                      b). a hard or soft centre                      c). a soft or chewy centre  
 d). a hard or chewy centre                      e). **not** a soft centre                      f). **not** a soft or hard centre ?

- 12). In a class of thirty pupils 8 play hockey, 10 play football, 4 play rugby and 8 go swimming. If a pupil is selected at random, what is the probability that the pupil will  
 a). play football                      b). play hockey or swim                      c). play hockey or football  
 d). **not** play rugby                      e). **not** swim                      f). **not** play rugby or swim ?

- 13). In a 50 pence cash bag there are ten 1 pence coins, five 2 pence coins, four 5 pence coins and one 10 pence coin. If a coin is drawn at random, what is the probability that the coin :-  
 a). is a 5p                      b). is a copper coin                      c). is **not** a 5p or 10p  
 d). is a 1p or a 5p                      e). is **not** a copper coin                      f). is **not** a 1p, 2p or 5p ?

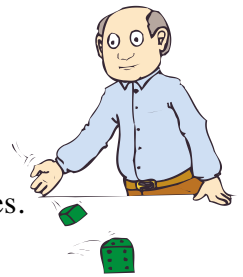
- 14). A box contains 2 blue discs, 14 green discs and 4 red discs. If a disc is picked at random what is the probability of getting :-  
 a). a blue disc                      b). a green disc                      c). a blue or red disc  
 d). a blue or green disc                      e). **not** a green disc                      f). a blue, green or red disc?







## Assigning Probabilities.



We cannot always assign a probability to an event using equally likely outcomes.  
Another way to assign a probability is to do an experiment or survey.

**When we conduct our experiment or survey the bigger the sample the more accurate the results!**

### Surveys.

- 1). In this survey we will find the probability that the next car passing the school is red.  
a). Copy and complete the table below.

Car Colour	Tally	Freq.
Red		
Not Red	Lots of space will be needed for Not Red!	
	Total	

- b).  $P(\text{next car is red}) = \frac{\text{Number of red cars}}{\text{Total of cars in survey}} = \frac{\quad}{\quad}$  (Cancel this down if you can).

Conduct a survey that will find the following probabilities :-

- 2). that the next vehicle passing the school is a bus.  
3). that the next person I meet in school likes netball as their favourite sport.  
4). that the next person I meet in school has school dinners.



### Experiments.

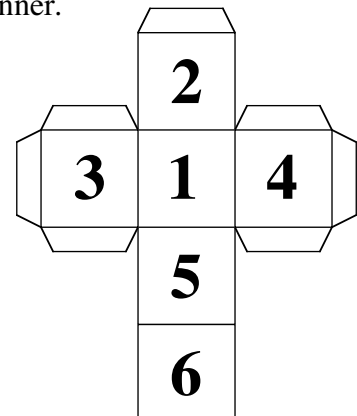
- 1). In this experiment we will find the probability of a drawing pin landing point down when dropped on to the table 150 times.  
a). Copy and complete the table below.

Outcome	Tally	Freq.
Point down		
Point up		
	Total	

- b).  $P(\text{Point down}) = \frac{\text{Number of Point down}}{\text{Total number of drops}} = \frac{\quad}{\quad}$  (Cancel this down if you can).

- 2). Cut out your own spinner from cardboard. **Do not make a regular shape.** Mark off sectors and label them with numbers. Push a matchstick through the centre. Secure this with blu-tac if it is wobbly! You now have your own unique spinner.  
Find the probabilities of it landing on each sector for 200 spins.

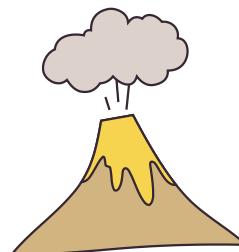
- 3). Make your own biased die. Copy the net on to squared paper. Cut it out. Now add a small piece of blu-tac to one of the sides. Make sure this is firmly attached and will not fall off. This will weigh the die down to one side and make it biased.  
Now make the die.  
Roll it 200 times and find the probabilities of it landing on each side.



## Look Back at Data.

Sometimes we cannot do a survey or experiment because the events happen infrequently. For example you would not sit watching a volcano to see if it erupted. You would look back at data in newspapers and journals.

- A -- Use equally likely outcomes.
- B -- Look back at data.
- C -- Use a survey or experiment to collect data.



Which of the above methods would you use to find :-

- 1). The probability a particular country will have an earthquake next year.
- 2). The probability a person chosen at random in a sports club will be left handed.
- 3). The probability a **biased die** will land on 6 when rolled.
- 4). The probability a girl's name will be picked at random out of 50 girls and 50 boys.
- 5). The probability that a car is broken into on a Saturday night in London.
- 6). The probability a shoe pushed off a desk will land the right way up.
- 7). The probability a **fair die** will land on 6 when rolled.
- 8). The probability that I win a raffle if I buy 10 out of the 150 tickets on sale.
- 9). The probability that it will snow on Christmas day.
- 10). The probability that a diamond will be chosen from a pack of cards.



## Theory v Experiment.

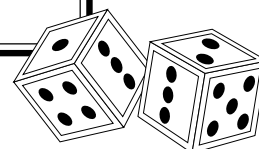
In this section we will compare probability theory with our experiments.

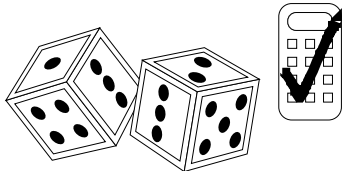
**Where the answer is a probability, leave it as a decimal** - it will be easier to compare results.

- 1). Throwing a coin.
  - a). What is the probability theory of throwing a coin and it landing on Heads ?
  - b). If I throw the coin 200 times how many times would I expect it to land on Heads ?
  - c). Now throw a coin 200 times and record your results.
  - d). Are the results exactly as the theory said ?  
What experimental probability did you get for landing on Heads ?
  - e). Put your class results together. What experimental probability did the class get as a whole ? Was this better than yours on its own ?
- 2). Rolling a die.
  - a). What is the probability theory of rolling a die and it landing on number 2 ?
  - b). If I roll the die 120 times how many times would you expect it to land on number 2 ?
  - c). Now roll the die 120 times and record your results.
  - d). Are the results exactly as the theory said ?  
What experimental probability did you get for landing on 2 ?
  - e). Put your class results together. What experimental probability did the class get as a whole ? Was this better than yours on its own ?

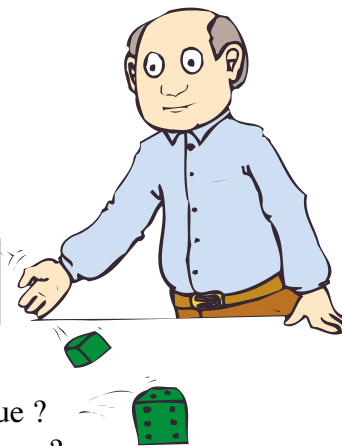


**The more times you do an experiment the closer the results get to the theoretical probability.**





## Experimental Probabilities.



1). Here are the results of a survey of cars passing the school.

Colour	Red	Blue	Green	Yellow	Other
Number of cars	40	30	15	10	5

- a). What is the probability of the next car passing the school being:-
  - i). red;
  - ii). green;
  - iii). yellow;
  - iv). **not** blue ?
- b). If 900 cars pass the school, how many do you think would be yellow ?
- c). If 60 cars pass the school, how many do you think would be red ?
- d). If 400 cars pass the school, how many do you think would be blue ?

2). A drawing pin is repeatedly dropped in an experiment to see which way up it will land. Here are the results.

Outcome	Frequency
Point up	160
Point down	40

- a). What is the probability of the drawing pin landing
  - i). point up;
  - ii). point down ?
- b). If the drawing pin is dropped 600 times how many times do you think it would land point up ?
- c). If the drawing pin is dropped 50 times how many times do you think it would land point down ?

3). Jean conducts a survey on pupils' favourite snacks. Here are the results:-

Snack	Crisps	Chocolate	Fruit	Biscuit	Other
Frequency	30	25	8	40	17

- a). What is the probability of a pupil:-
  - i). liking Crisps;
  - ii). liking Fruit;
  - iii). liking Biscuits;
  - iv). **not** liking chocolate?
- b). If 600 pupils were asked, how many would say they preferred a biscuit ?
- c). If 80 pupils were asked, how many would say they preferred crisps ?
- d). If 360 pupils were asked, how many would say they preferred chocolate ?

4). In an experiment, 20 seeds are sown, but only 14 germinate.

- a). What is the experimental probability of a seed:-
  - i). germinating;
  - ii). not germinating ?
- b). If 60 seeds are sown, what number might be expected to germinate ?

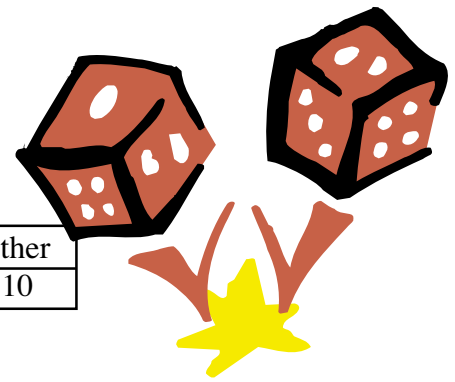


5). 50 trains arrived at Bolton Station this morning. 12 arrived early, 8 were late and the rest were on time.

- a). What is the probability that the next train will be:-
  - i). late;
  - ii). early;
  - iii). on time ?
- b). 15 trains arrive in the afternoon, how many would you expect on time ?
- c). Tomorrow 75 trains are due, how many would you expect to be early ?
- d). This week 825 trains should come through Bolton Station, how many would you expect to be late ?

6). Here are the results of a survey of favourite colours in Year 7.

Colour	Red	Blue	Green	Yellow	Other
Frequency	80	26	34	30	10



- a). What is the probability that a pupil's favourite colour is:  
 i). red;    ii). green;    iii). yellow;    iv). **not** blue ?  
 b). If 720 pupils are asked, how many do you think would say red ?  
 c). If 24 pupils are asked, how many do you think would say yellow ?  
 d). If 90 pupils are asked, how many do you think would say blue ?

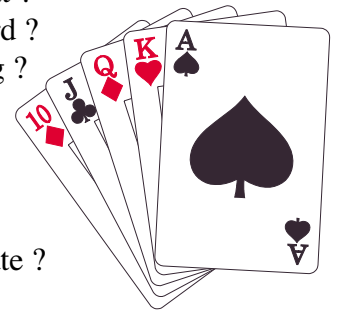
7). Andrew and Gordon conduct a survey on pupils' favourite pets. Here are the results:-

Pet	Cat	Chimp	Dog	Bird	Other
Frequency	16	4	24	3	1

- a). What is the probability of a pupil's favourite pet being:-  
 i). a cat;    ii). a chimp;    iii). a bird;    iv). **not** a dog?  
 b). If 270 pupils were asked, how many would say they preferred a cat ?  
 c). If 464 pupils were asked how many would say they preferred a bird ?  
 d). If 38 pupils were asked, how many would say they preferred a dog ?

8). In an experiment, 92 seeds are sown, but only 69 germinate.

- a). What is the experimental probability of a seed :-  
 i). germinating;    ii). not germinating ?  
 b). If 552 seeds are sown, what number might be expected to germinate ?



9). A Police car stops 100 cars at random. 8 drivers had not paid their road tax, 3 others had no insurance and 4 others had invalid MOT certificates. The rest of the cars had everything in order.

- a). What is the probability of a driver's documents being in order ?  
 b). The next day the police car stops 300 cars, how many might they expect to have no insurance ?

10). 60 buses arrived at Bury Terminal this morning. 15 arrived early, 10 were late and the rest were on time.

- a). What is the probability that the next bus will be:-  
 i). late;    ii). early;    iii). on time ?  
 b). 48 buses arrive in the afternoon, how many would you expect on time ?  
 c). Tomorrow 108 buses are due, how many would you expect to be early ?  
 d). This week 696 buses should come through Bury Terminal. How many would you expect to be late ?

11). On average, 3 out of 100 households have no television, 21 have a black and white set, and the rest have a colour television set. If a school has 800 families, find:-

- a). the probability of a pupil having a colour television set at home,  
 b). how many of the families might have a colour television set,  
 c). how many of the families might have no television set at all.

